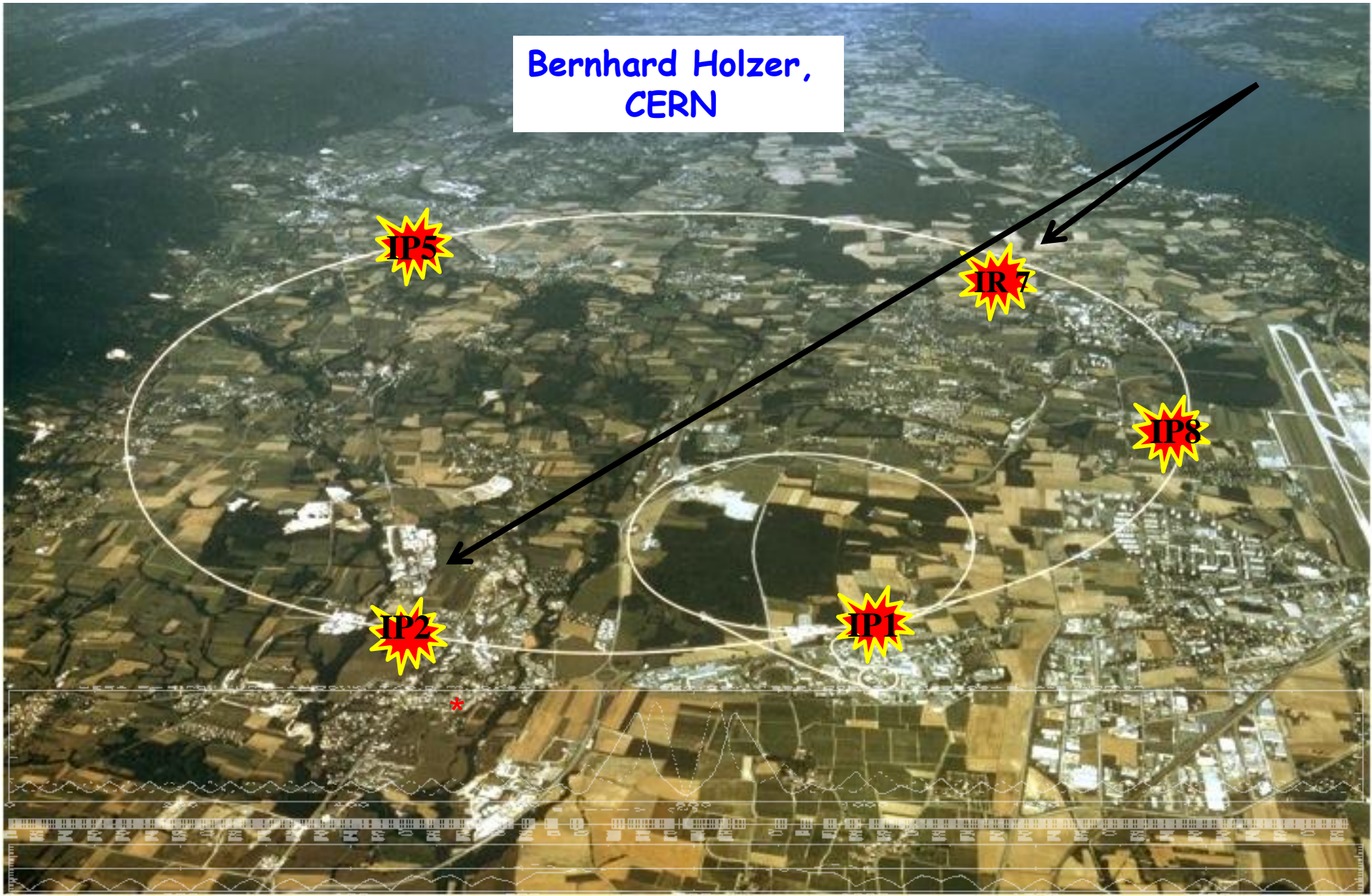


"Nb3Sn Dipoles in LHC ... a philosophical contemplation"

Bernhard Holzer,
CERN



"Nb₃Sn Dipoles in LHC

... a philosophical contemplation"

Doctor of Philosophy, abbreviated to **PhD** in English-speaking countries:

Greek *διδάκτωρ φιλοσοφίας*

Here φιλοσοφία/philosophy, literally translating to "the love of wisdom", is used in the original Greek sense, loosely meaning "the pursuit of in depth knowledge".

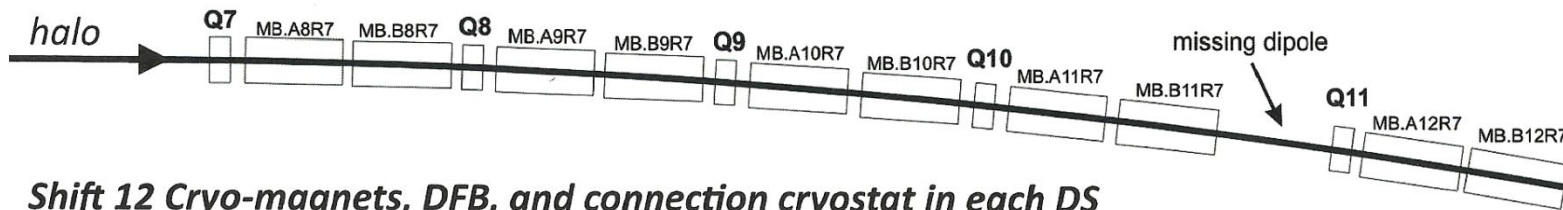
in other words

“Nb₃Sn dipoles in the LHC DS: preliminary results”

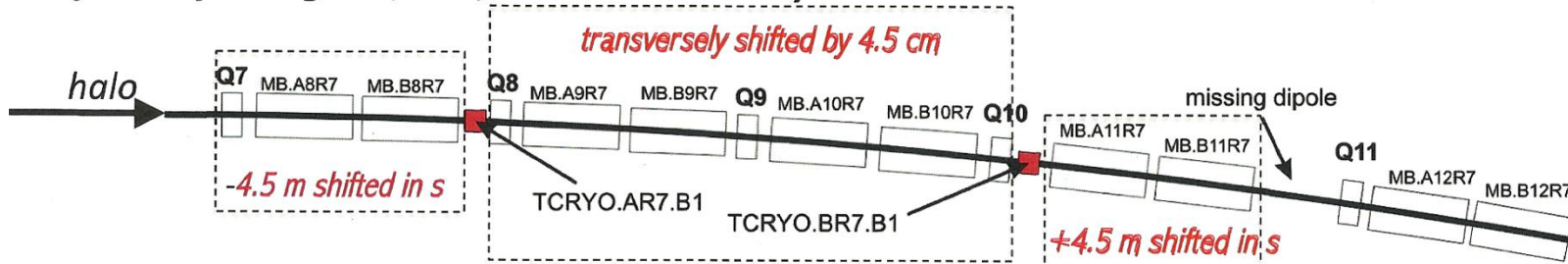
... what are we talking about ???

replace two standard dipoles in the dispersion suppressor region
by stronger \leftrightarrow shorter Nb₃Sn dipoles to gain space for Ralph

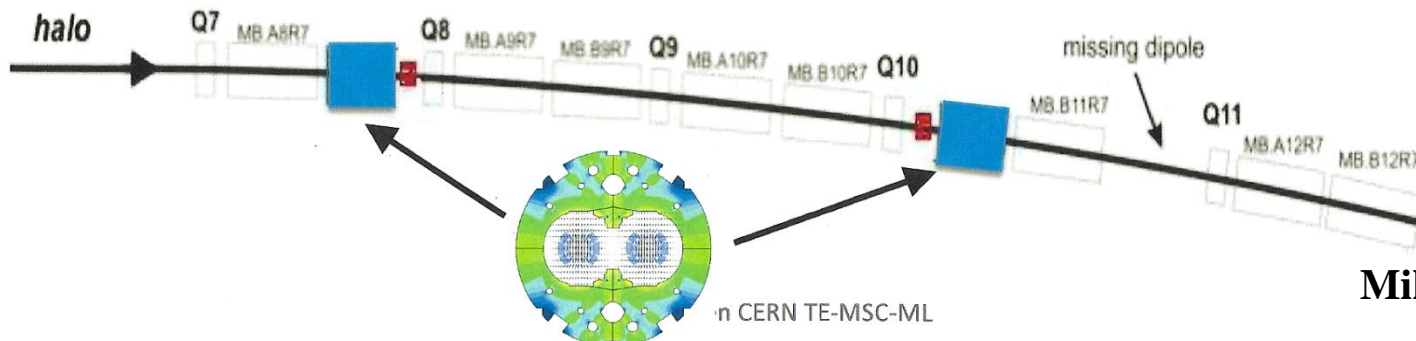
DS Upgrade Scenarios



Shift 12 Cryo-magnets, DFB, and connection cryostat in each DS



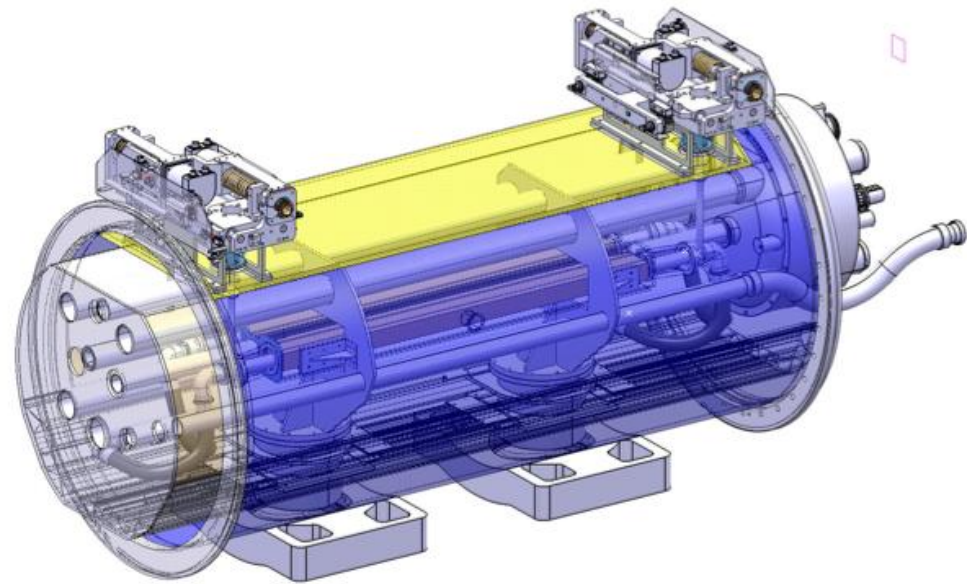
New 3..3.5 m shorter Nb₃Sn Dipoles (2 per DS)



© CERN TE-MSC-ML

Mikko Karppinen

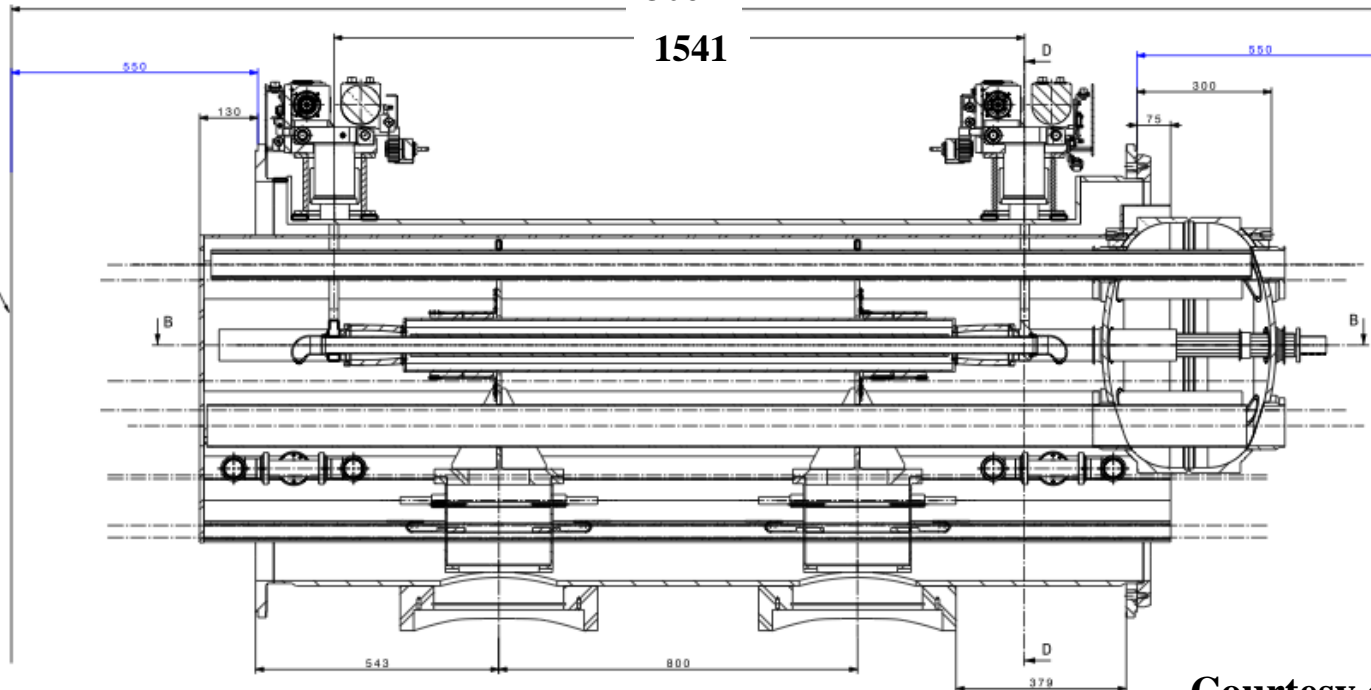
Cryo-collimator



3061

1541

PLAN
INTER-CONNECTION
UPSTREAM



Section view A-A
Scale: 1:5

PLAN
INTER-CONNECTION
DOWNSTREAM

Courtesy of D. Ramos

Effects to be expected:

- * magnets are shorter than MB Standards → change of geometry
distortion of design orbit
- * R-Bends ↔ S-Bends → edge focusing
distortion of the optics
tune shift, beta beat
- * nonlinear transfer function (3.5 TeV) → distortion of closed orbit
to be corrected locally ??
dedicated corrector coils ??
trim power supply ??
- * feed down effects from sagitta ?
- * multipole effect on dynamic aperture ?

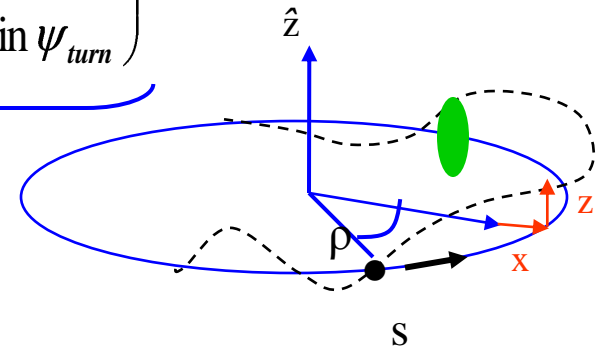
Analytical approach / Mad-X / Sixtrack Simulations

1.) R-Bernd / S-Bend: a (small) optics problem the “edge focusing”

Quadrupole Error in the Lattice

optic **perturbation** described by **thin lens quadrupole**

$$M_{dist} = M_{\Delta k} \cdot M_0 = \underbrace{\begin{pmatrix} 1 & 0 \\ \Delta k ds & 1 \end{pmatrix}}_{\text{quad error}} \cdot \underbrace{\begin{pmatrix} \cos \psi_{turn} + \alpha \sin \psi_{turn} & \beta \sin \psi_{turn} \\ -\gamma \sin \psi_{turn} & \cos \psi_{turn} - \alpha \sin \psi_{turn} \end{pmatrix}}_{\text{ideal storage ring}}$$

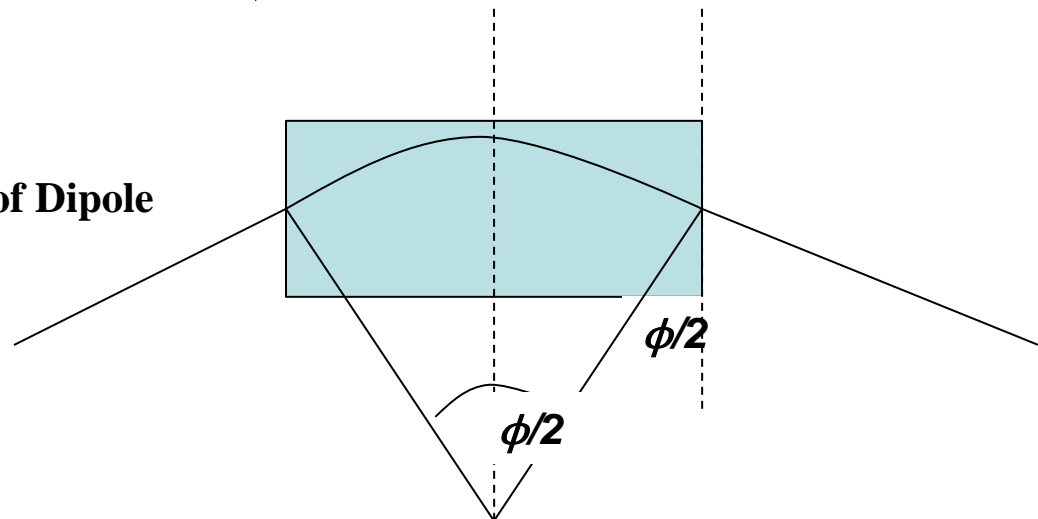


$$M_{dist} = \begin{pmatrix} \cos \psi_0 + \alpha \sin \psi_0 & \beta \sin \psi_0 \\ \Delta k ds (\cos \psi_0 + \alpha \sin \psi_0) - \gamma \sin \psi_0 & \Delta k ds \beta \sin \psi_0 + \cos \psi_0 - \alpha \sin \psi_0 \end{pmatrix}$$

Quadrupole Error in this case:

Edge Focusing effect of Dipole

$$M_{edge} = \begin{pmatrix} 1 & 0 \\ \frac{1}{\rho} \tan \frac{\phi}{2} & 1 \end{pmatrix}$$



Edge Foc Effect:

for the two effects (entrance / exit)
of two dipoles we obtain ...

$$\Delta Q \approx 1.39 \cdot 10^{-5}$$

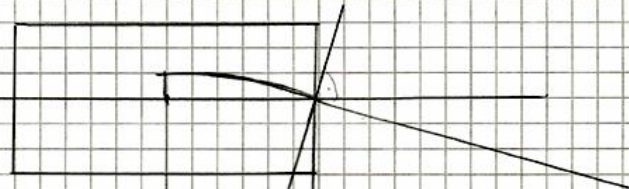
effect on beam optics is small !!!

Konstanten für den Effekt:

$$M = \begin{pmatrix} 1 & 0 \\ \frac{1}{f} & 1 \end{pmatrix}$$

ψ = Einfallswinkel gegen die Normale

β = Ablenkwinkel



$$\psi = \frac{\alpha}{2} = \text{gute Näherung}$$

$$Q \cdot \beta = p/c$$

$$Q = \frac{7 \cdot 10^{22} \text{ eV} \cdot \beta \text{ m}^2}{3 \cdot 10^8 \text{ m/s} \cdot 8.33 \text{ Vs}}$$

$$= \frac{7 \cdot 10^{14}}{3 \cdot 8.33}$$

$$=$$

Ablenkwinkel des MZ:

$$\alpha = \frac{20}{1232} = 5.1 \text{ mrad}$$

$$f = 280 \text{ cm}$$

$$l = 14.3 \text{ cm}$$

$$\beta = 8.33 \text{ T (750V)}$$

$$\Rightarrow \frac{1 \text{ cm} \cdot \psi}{f} = \frac{2 \cdot 4 \text{ cm} (5.1 \text{ mrad} / 2)}{280 \text{ cm}} = 1.8 \cdot 10^{-6}$$

Faktor 2
für Ein-
& Ausgang

Nachher: Matrix einer Overströy: $M = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

→ Transmitt: $\Delta Q = \frac{1}{h \cdot \beta} \cdot \text{ph. ds. } \beta$
↳ create durch $\frac{1 \text{ cm} \cdot \psi}{f}$

$$\Delta Q_1 \approx \frac{1}{h \cdot \beta} \cdot 50 \text{ m} \cdot 1.8 \cdot 10^{-6}$$

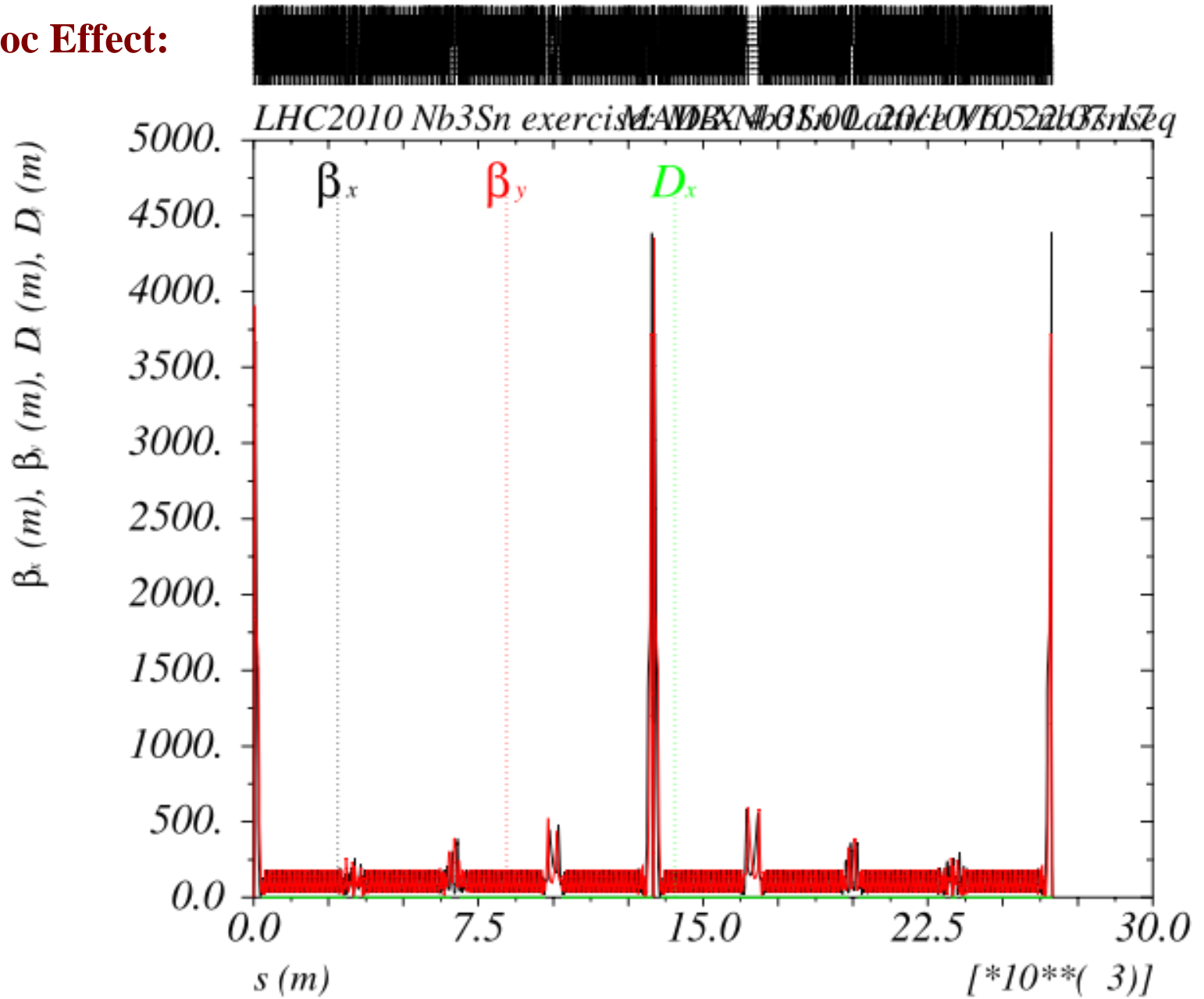
$$= 0.87 \cdot 10^{-5} \text{ für den 1. Magnet.}$$

Da es gibt 2 solche Magnete: der zweite bei $\beta = 36 \text{ m.}$

$$\Delta Q_2 \approx \frac{1}{h \cdot \beta} \cdot 36 \text{ m} \cdot 1.8 \cdot 10^{-6} = 0.516 \cdot 10^{-5}$$

$$\Rightarrow \Delta Q_{\Sigma} = 1.39 \cdot 10^{-5}$$

Edge Foc Effect:



Edge Foc Effect: optics distortion

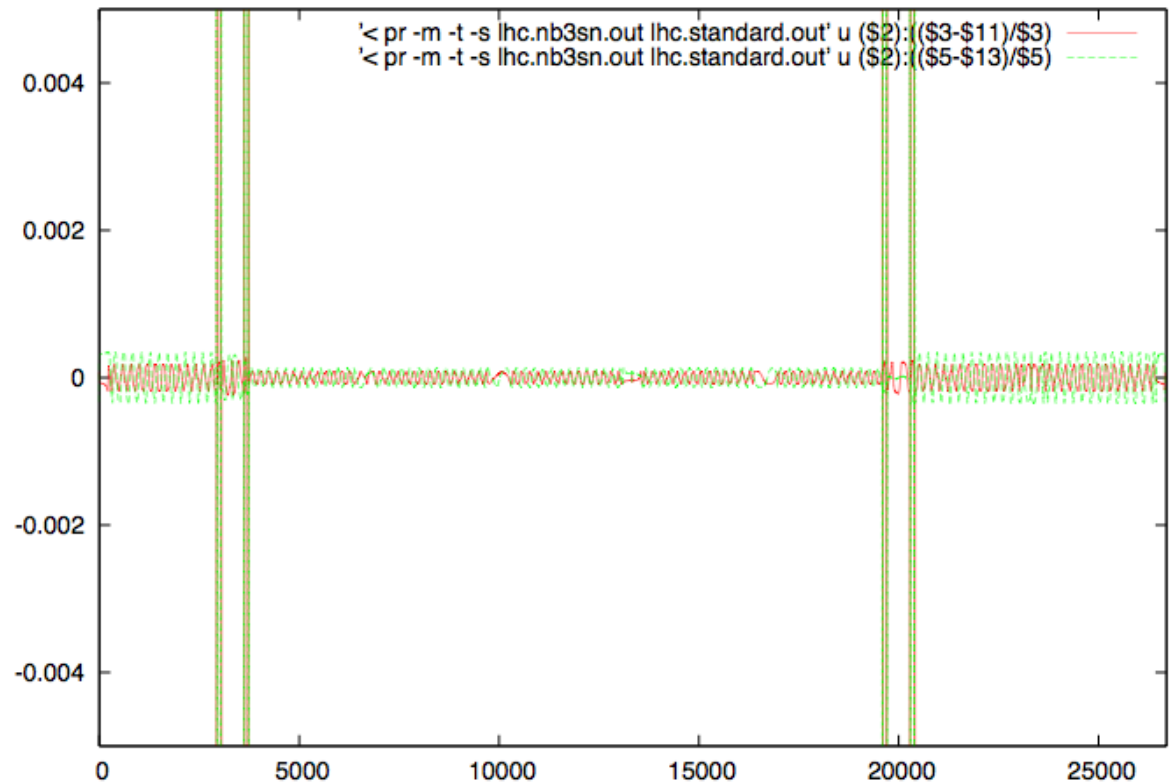
beta beat: $\Delta\beta/\beta < 1 * 10^{-3}$

tune shift: $\Delta Q_x \approx 9.05 * 10^{-5}$

$\Delta Q_y \approx 1.33 * 10^{-4}$

remember: analyt. result per magnet: :

$\Delta Q \approx 1.39 * 10^{-5}$



remember
tolerance for beta beat
 $\Delta\beta/\beta=20\%$

2.) Shorter Magnet: Change of Design Orbit

... global LHC geometry

Standard LHC

$$s = 26.6588832$$

$$x = 0.1217 \text{ mm}$$

$$z = 7.97 * 10^{-5} \text{ mm}$$

$$\theta = 6.2831$$

Nb₃Sn LHC

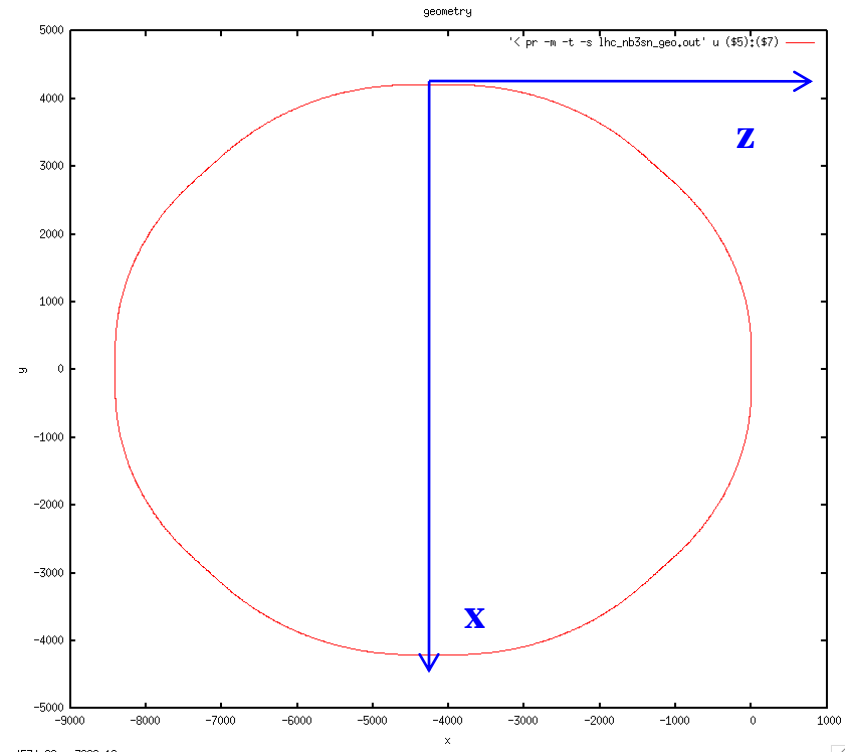
$$s = 26.65888319999$$

$$x = 0.228 \text{ mm}$$

$$z = 0.177 \text{ mm}$$

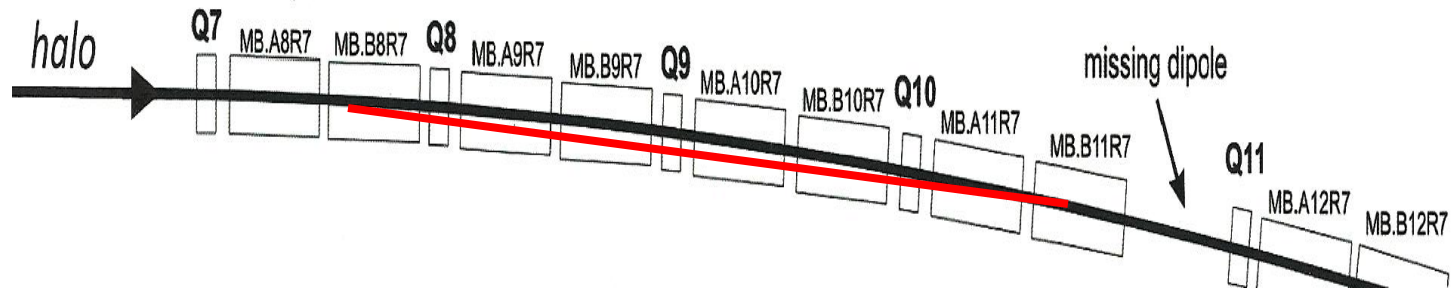
$$\theta = 6.2831$$

it's still quite a ring !!



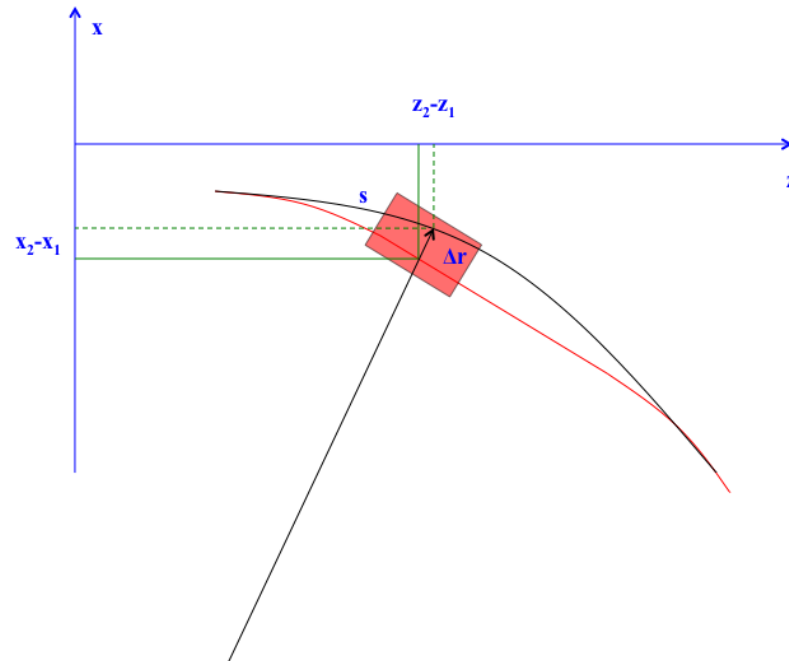
2.) Shorter Magnet: Change of Design Orbit

... local geometry

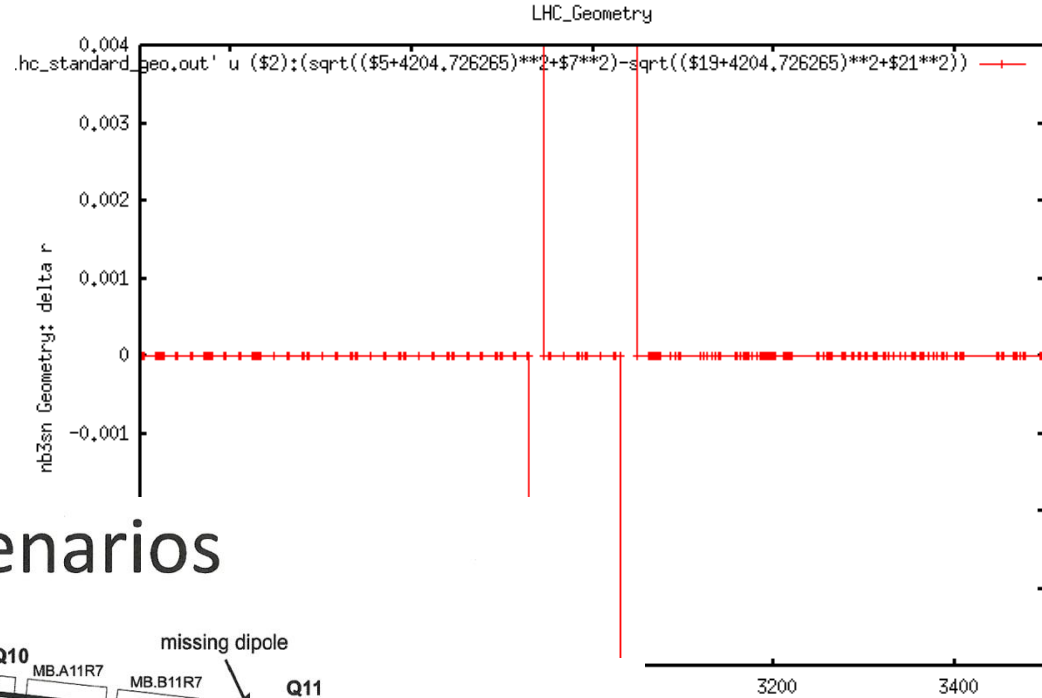


do we need a radial re-alignment
?

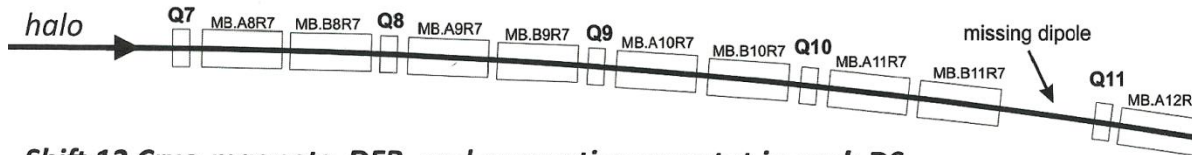
mad-x "Survey"



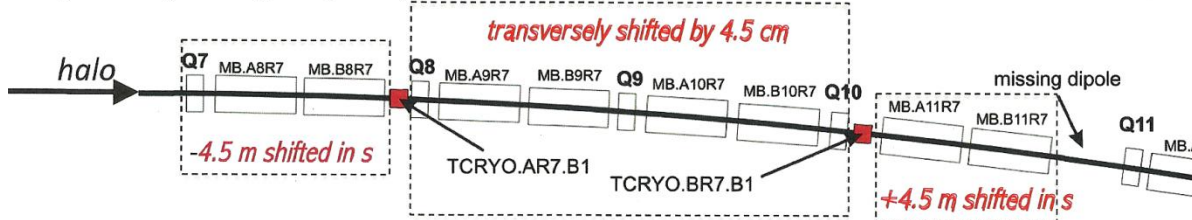
mad-x "Survey"



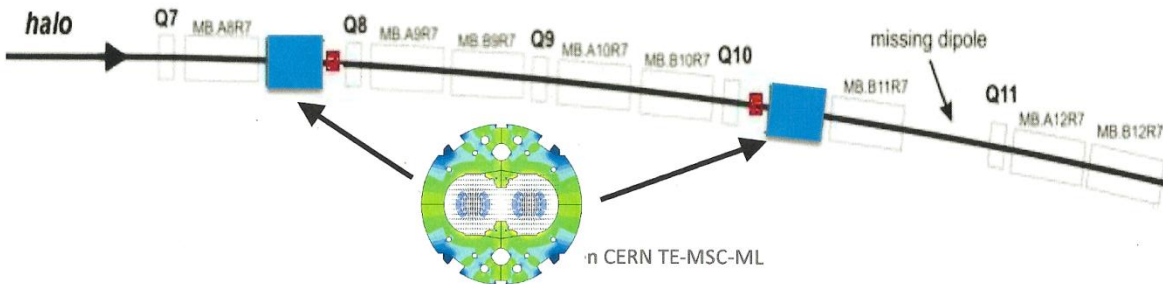
DS Upgrade Scenarios



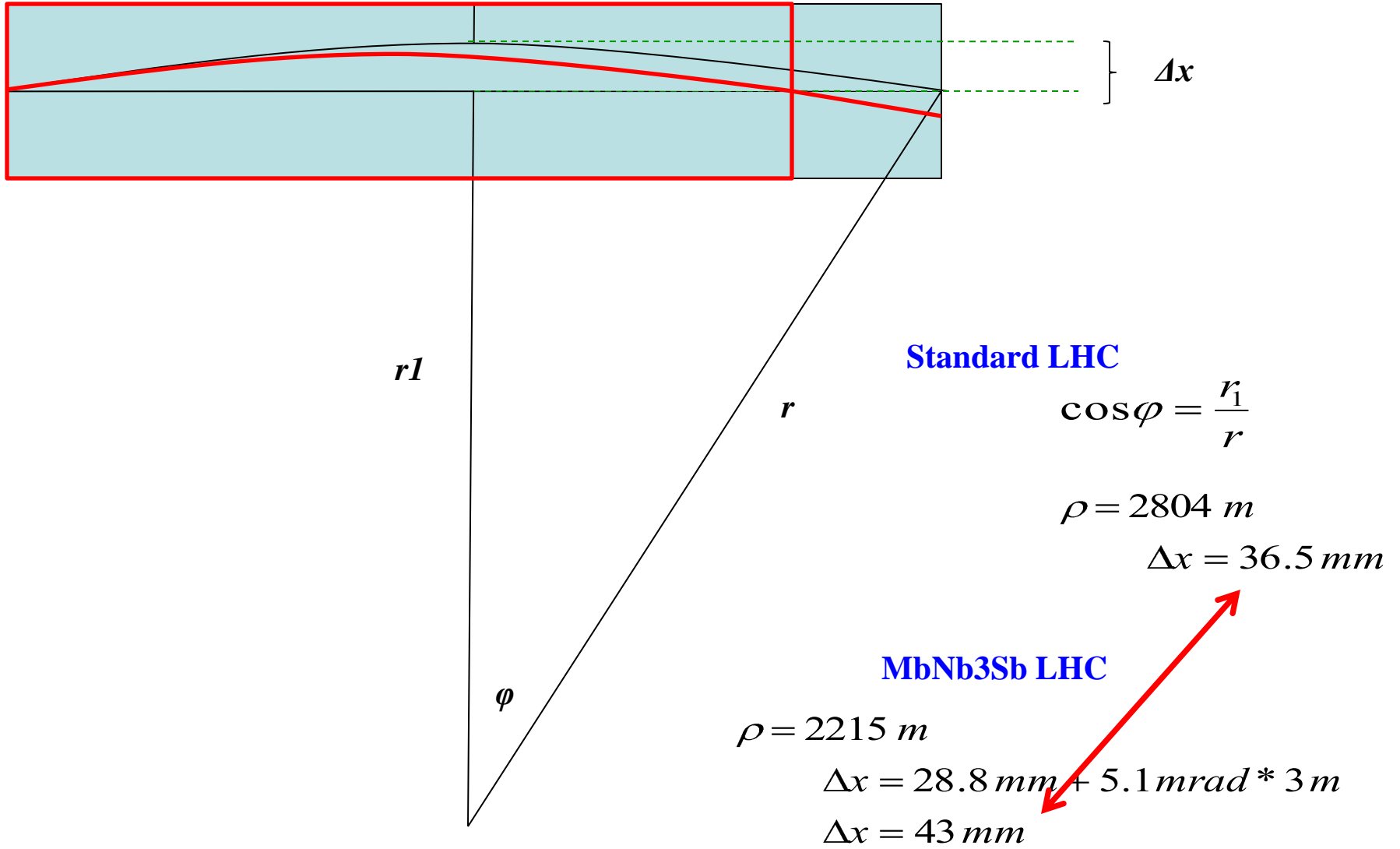
Shift 12 Cryo-magnets, DFB, and connection cryostat in each DS



New 3..3.5 m shorter Nb3Sn Dipoles (2 per DS)

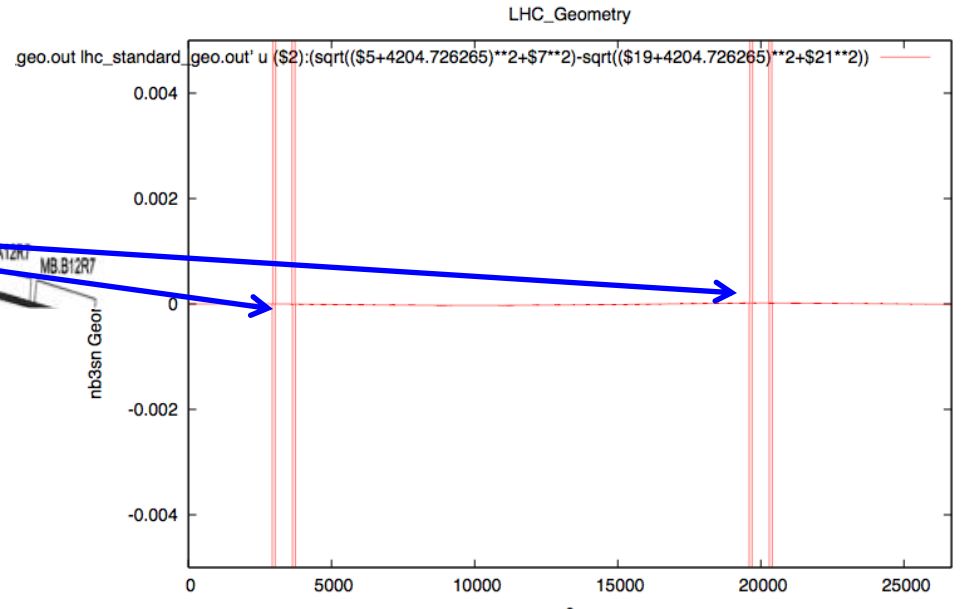
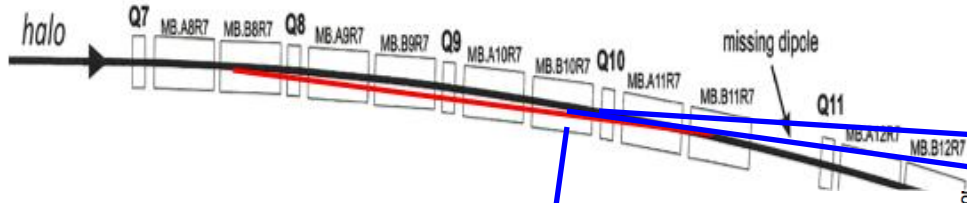


Attention !!!!
the exact position
of the MBNB's has
to be defined carefully

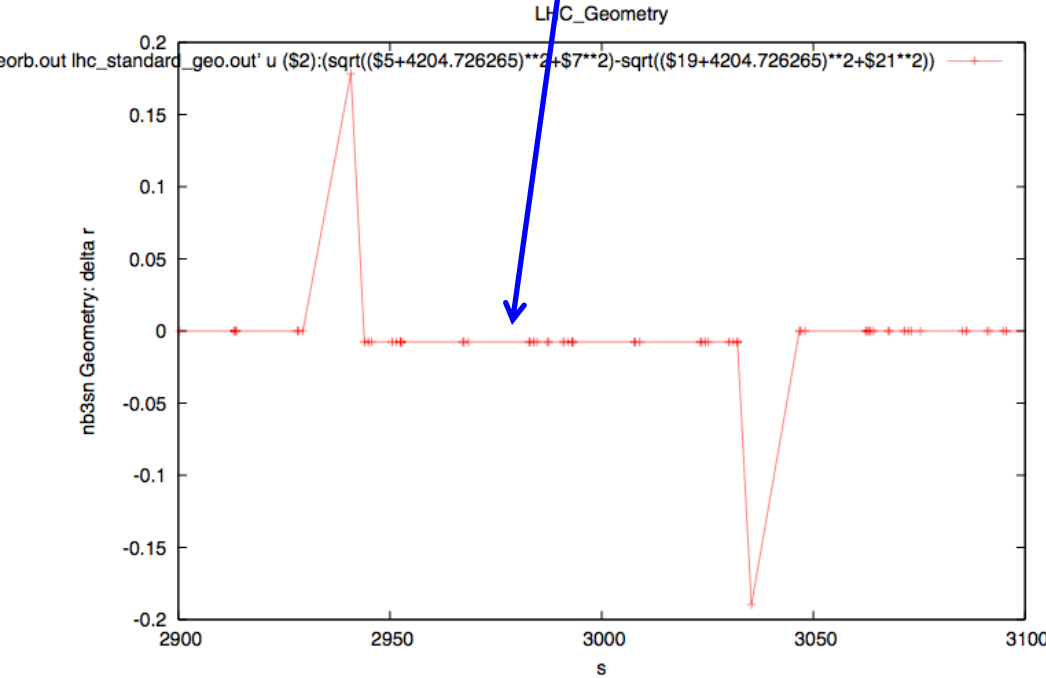


We expect a difference of $\approx 6.5 \text{ mm}$!!!!

mad-x “Survey”

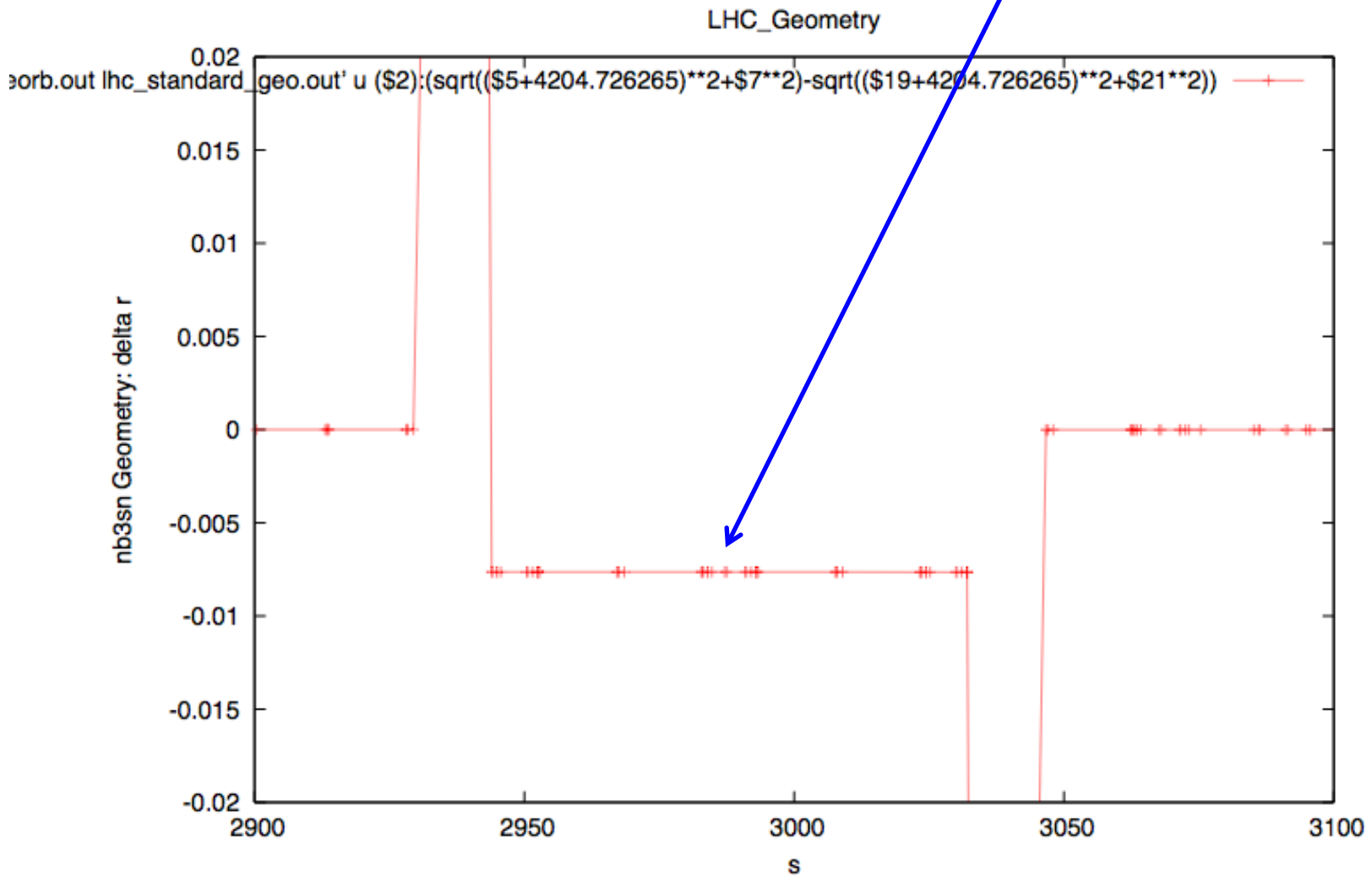
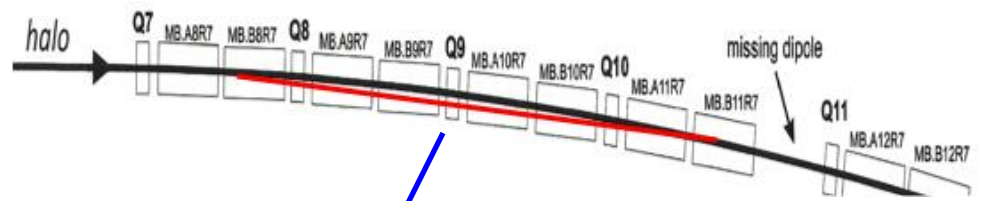


**difference in radial coordinate
standard LHC – Nb3Sn LHC
global result**



**difference in radial coordinate
standard LHC – Nb3Sn LHC
local at IP2**

difference in radial coordinate
 standard LHC – Nb3Sn LHC
 local result



3.) Sagitta:

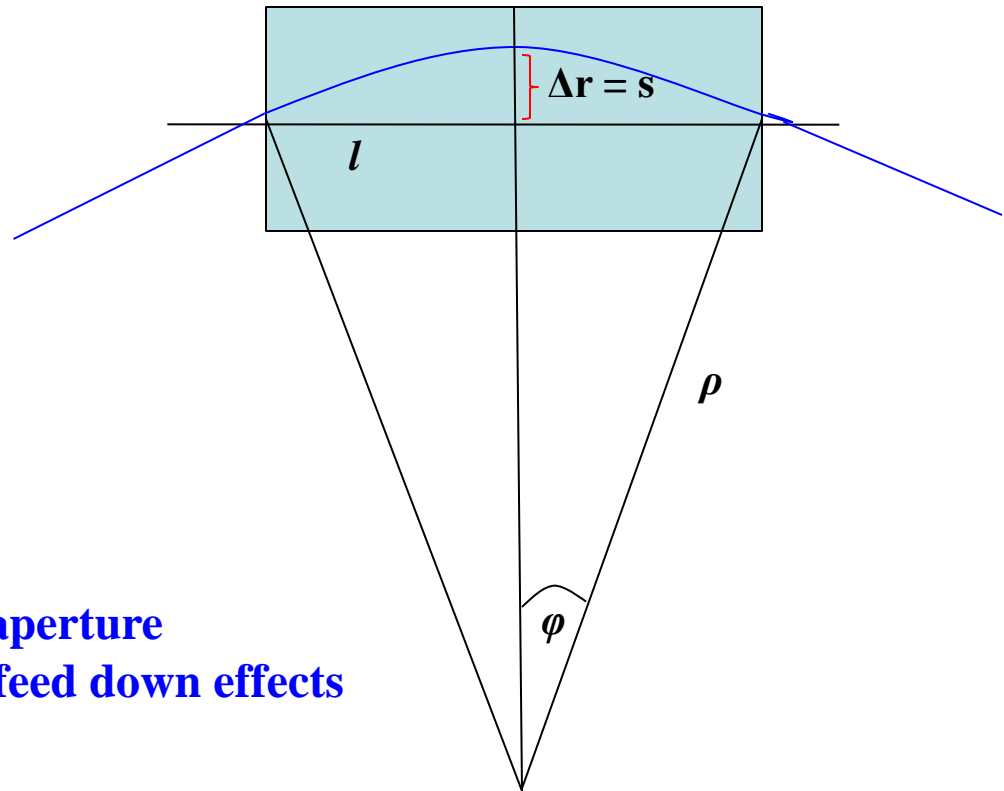
$$l = 11.3 \text{ m}$$

$$\rho = 2215 \text{ m}$$

$$\alpha = 2 * \varphi = 5.1 \text{ m rad}$$

$$s = r - \sqrt{r^2 - \frac{l^2}{4}} = 7 \text{ mm}$$

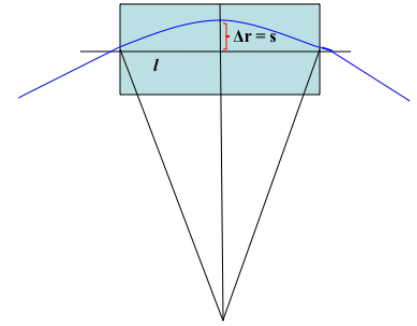
→ aperture
→ feed down effects



Feed Down Effects: $k_1 * l = \Delta x * l * \frac{1}{B\rho} * \frac{2B_0 b_3}{r_0^2}$

	Bdl	I	$b_{3(\text{syst})}$	$b_{3(\text{pc})}$	Σb_3	$B\rho$
450 GeV	7.7 Tm	758 A	13.96	+95.8	109.8	$1.5 * 10^3 \text{ Tm}$
3.5 TeV	59.6 Tm	5639 A	13.99	-4.72	9.27	$1.2 * 10^4 \text{ Tm}$
7 TeV	119.1 Tm	11517 A	13.37	+0.44	13.81	$2.3 * 10^4 \text{ Tm}$

Feed Down Effects:



Quadrupole Error: $k_1 * l = \Delta x * l * \frac{1}{B\rho} * \frac{2B_0 b_3}{r_0^2}$

Tuneshift: $\Delta Q = \frac{1}{4\pi} \int \beta k ds$

Beta Beat $\frac{\Delta\beta}{\beta} \approx \frac{1}{2 \sin 2\pi Q} \int \beta k ds$

	$k_1 l$	ΔQ	$\Delta\beta/\beta$
450 GeV	$2.79 * 10^{-3}$	0.031	20%
3.5 TeV	$2.35 * 10^{-4}$	0.00262	1.76%
7 TeV	$2.41 * 10^{-4}$	0.00268	1.80%
Phase 1 D1	$b_3 = 3 * 10^{-4}$	0.0059	3.9%

per Magnet

←
**considered as
tolerance limit (DA)**

4.) The Story of the Transfer Function ... a closed orbit problem

calculate the ideal (nb3sn) machine

flatten the experiment bumps, switch off LHC-B, ALICE etc

assign field error to nb3sn dipoles

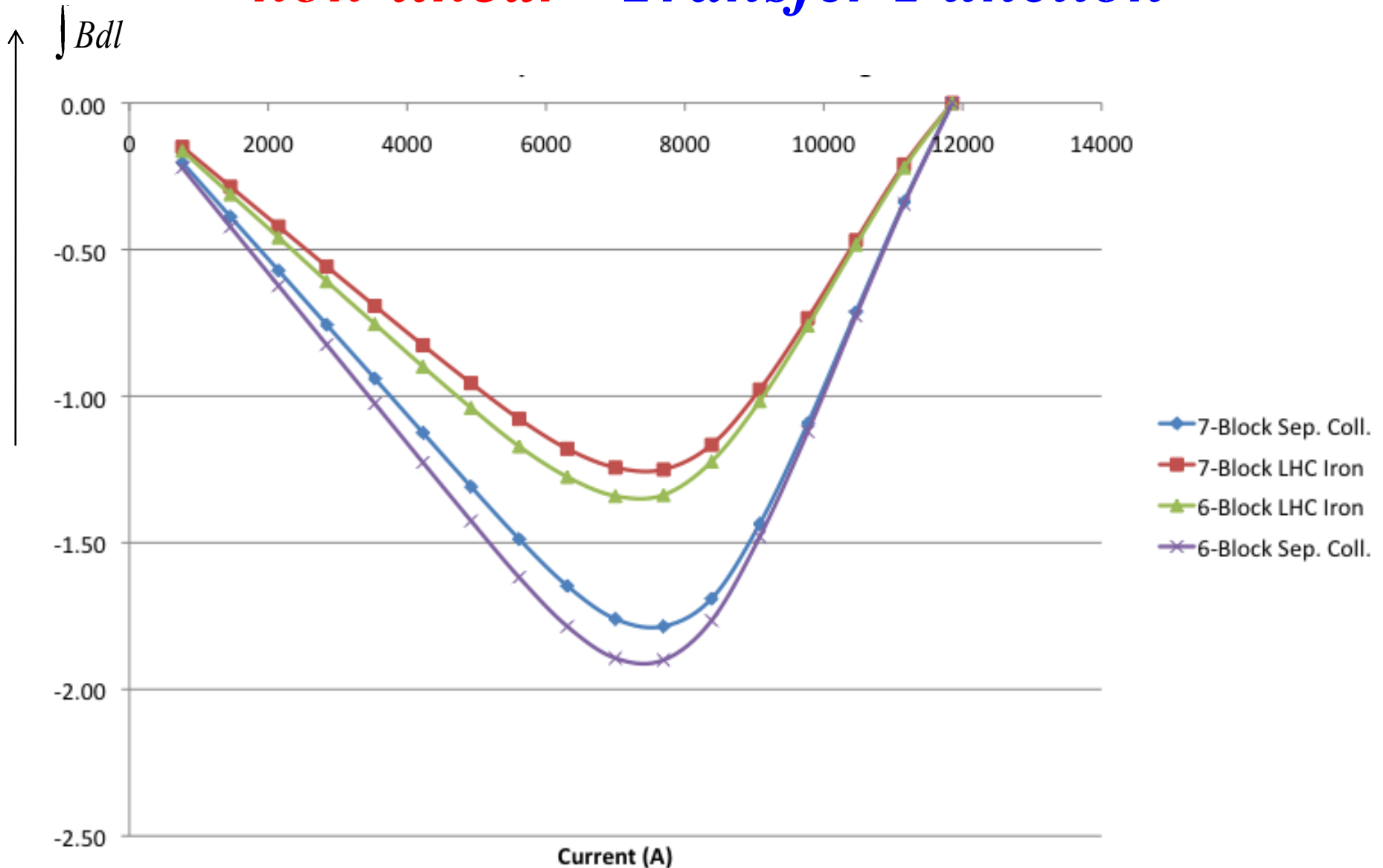
correct the orbit

plot the residual error

what are we talking about ... $\int Bdl = 1.5 \text{ Tm}$

treated not as a geometrical problem but as a orbit problem → can be corrected.

“non-linear” Transfer Function



again: ... 10 seconds for the contemplation:



$$\left. \begin{array}{l} E = 7 \text{ TeV} \\ B = 8.33 \text{ T} \\ L = 14.3 \text{ m} \end{array} \right\} \int Bdl = 119 \text{ Tm}$$

$N = 1232 \text{ Magnets}$

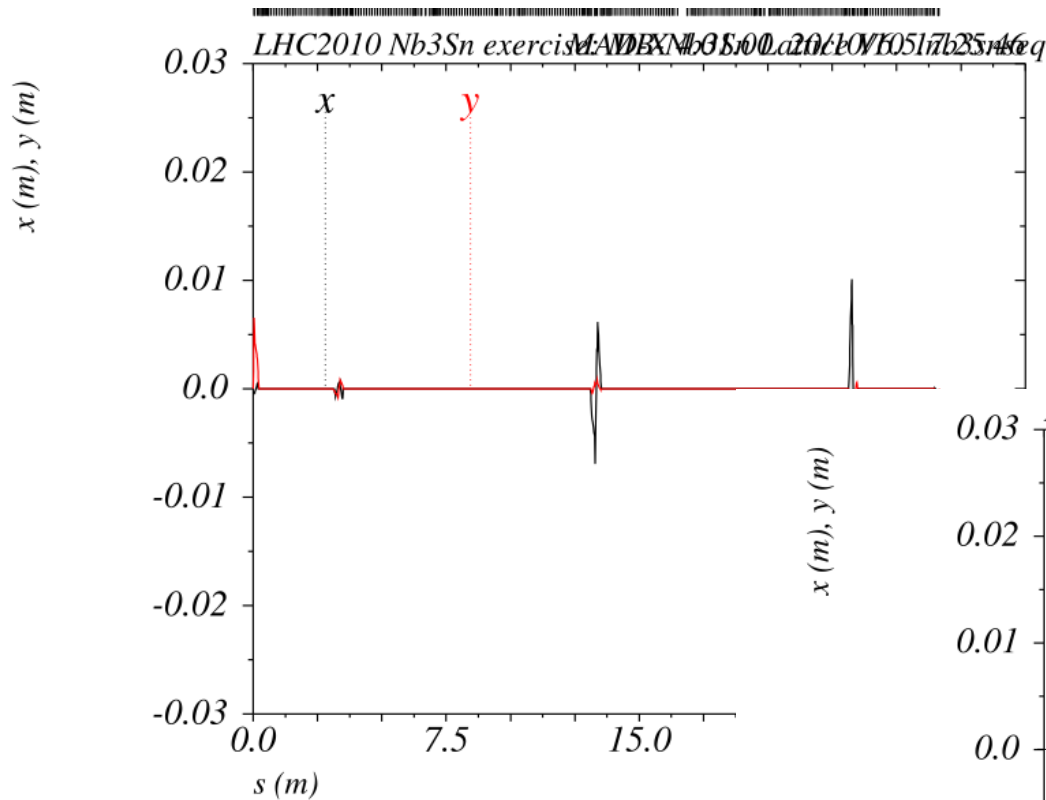
$\rightarrow 5.1 \text{ mrad}$

Nb3Sn Transferfunction:

worst case (... around 3.5 TeV) = **2.7% lack in main field**

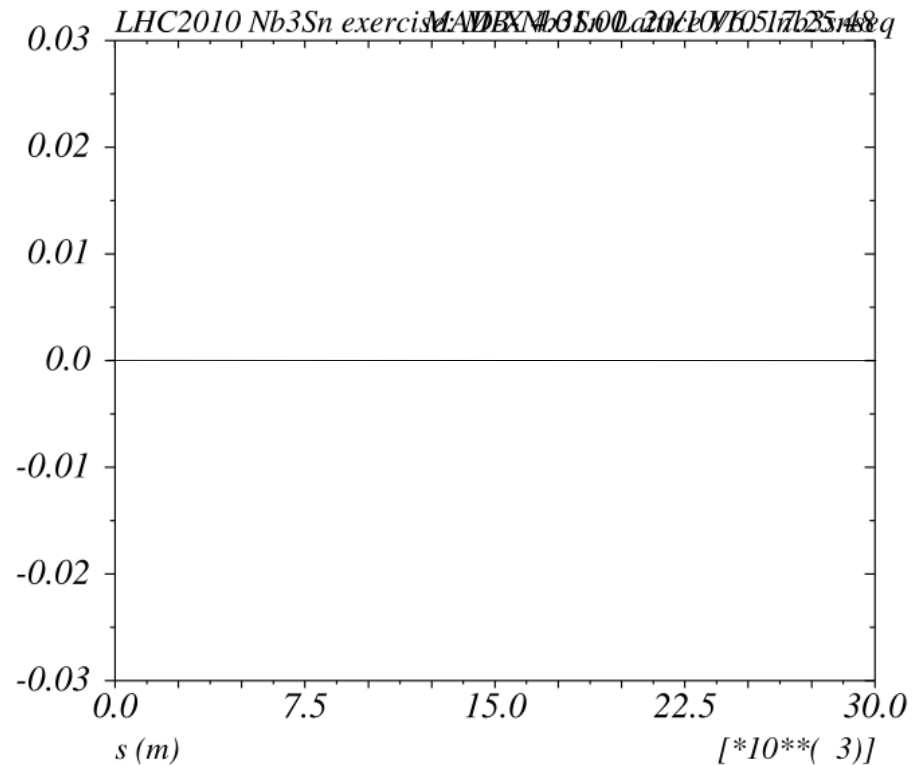
rough estimate: $\rightarrow \Delta x \approx 13 \text{ mm}$

4.) The Story of the Transfer Function ... a closed orbit problem



**ideal machine
with exp bumps**

... and without exp bumps



4.) The Story of the Transfer Function ...

a closed orbit problem

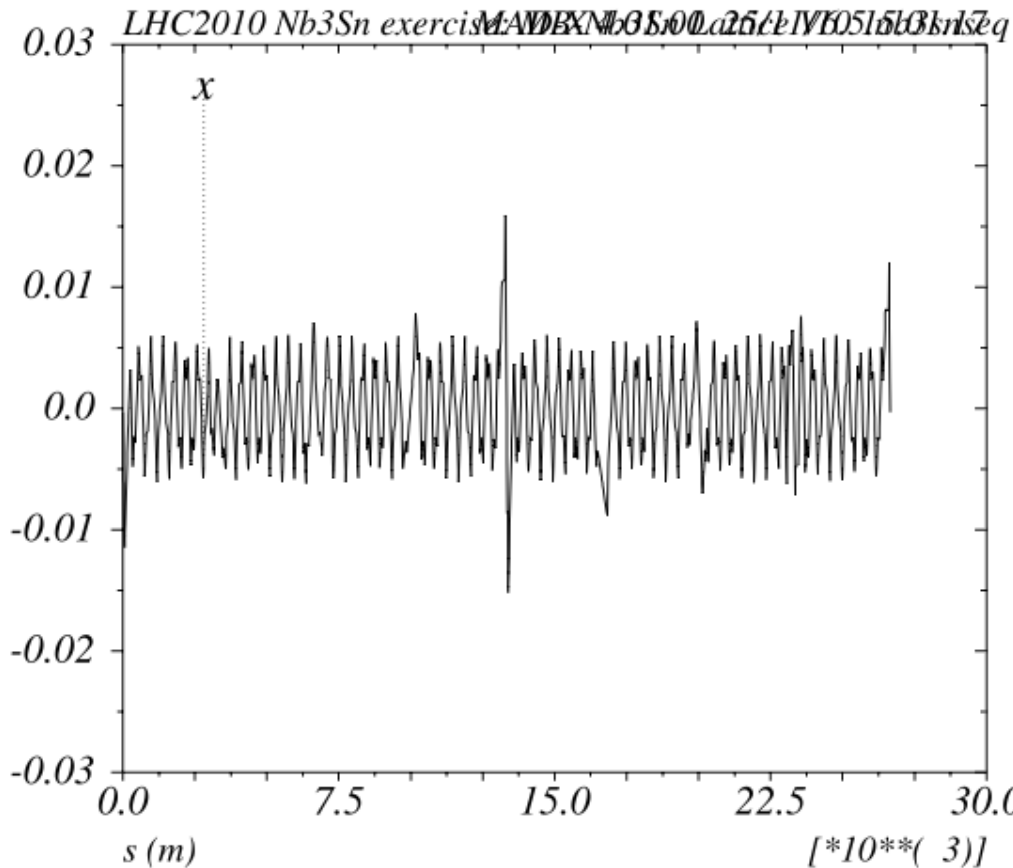
effect of nb3sn field error (1.5 Tm)

two dipoles

distorted orbit,

but partially compensated in a closed 180 degree bump

$\Delta\Phi = 4.545 \approx \text{modulo } 180 \text{ degree}$

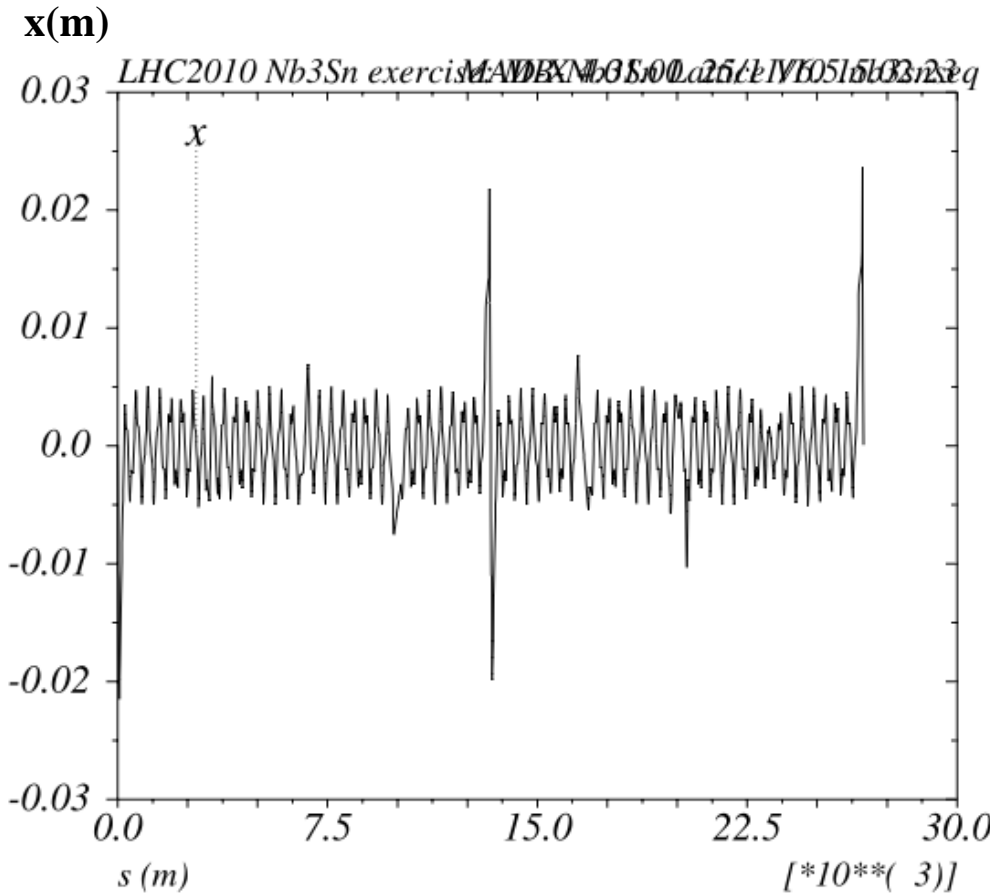


one Nb3Sn magnet

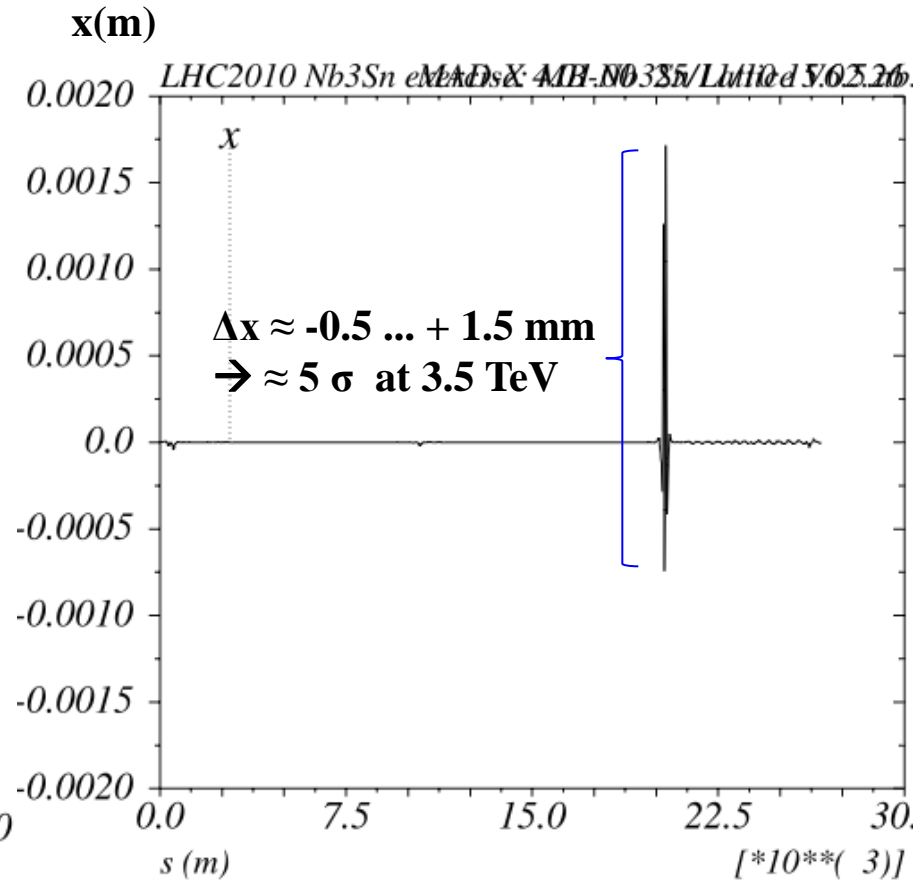
$\Delta x \approx \pm 15 \text{ mm}$

4.) The Story of the Transfer Function ... a closed orbit problem

effect of nb3sn field error (1.5 Tm)
two dipoles
distorted orbit,
and corrected by the “usual methods”



two Nb3Sn magnets

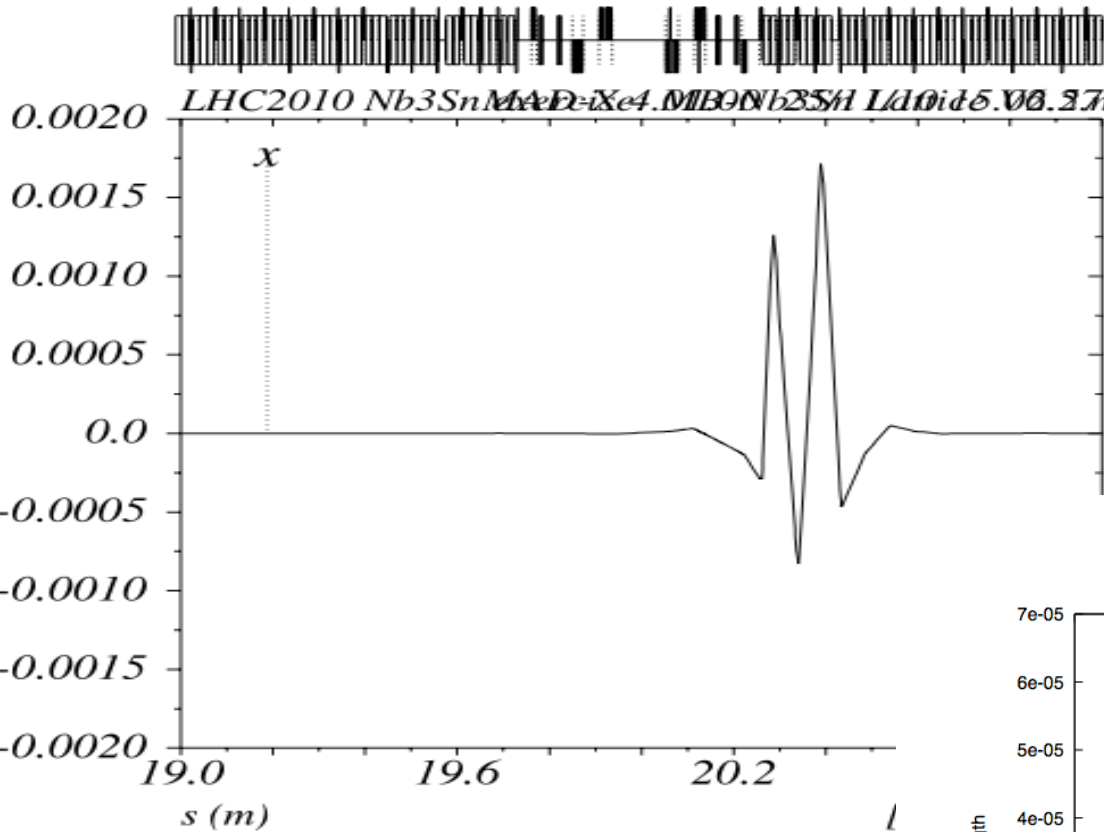


corrected by 20 orbcor dipoles

4.) The Story of the Transfer Function ... a closed orbit problem

field error corrected by 3 (20) most
eff. correctors
zooming the orbit distortion

... local distortion due to
 $\Delta\phi \approx 4.545$ phase relation,
closed by MCBH correctors

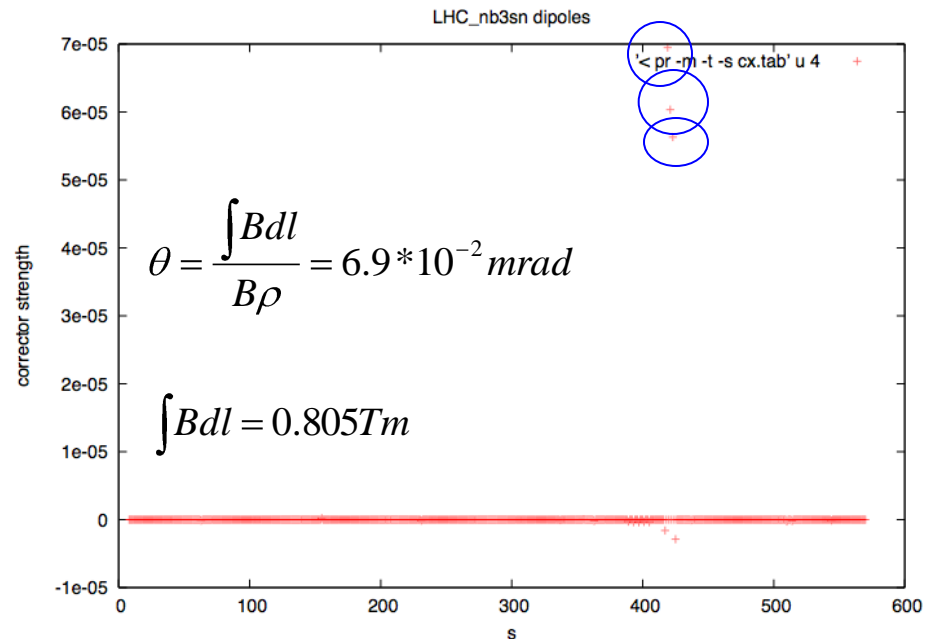


MCBH corrector strength:

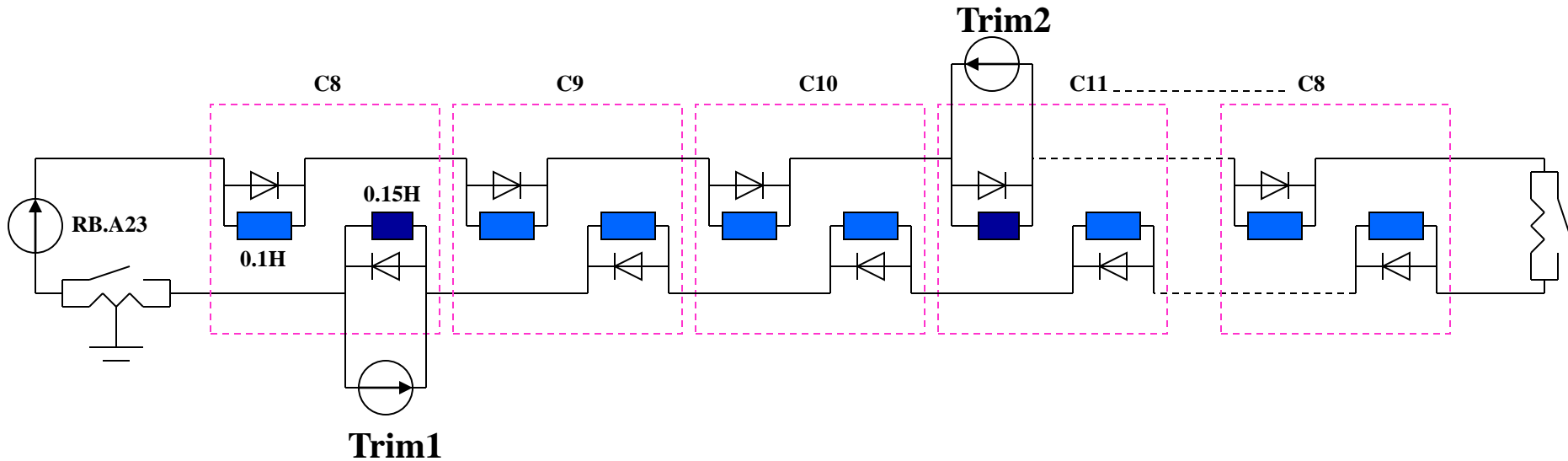
available: 1.900 Tm
needed: 0.805 Tm



= 42 %



New RB Circuit (Type 1)



Main Power Converter

Total inductance: 15.5 H ($152 \times 0.1\text{H} + 2 \times 0.15\text{H}$)

Total resistance: 1m Ω

Output current: 13 kA

Output voltage: 190 V

(+)

- Low current CL for the trim circuits
- Size of Trim power converters

TRIM Power Converters

Total inductance: 0.15 H

Total resistance: 1m Ω

RB output current: ± 0.6 kA

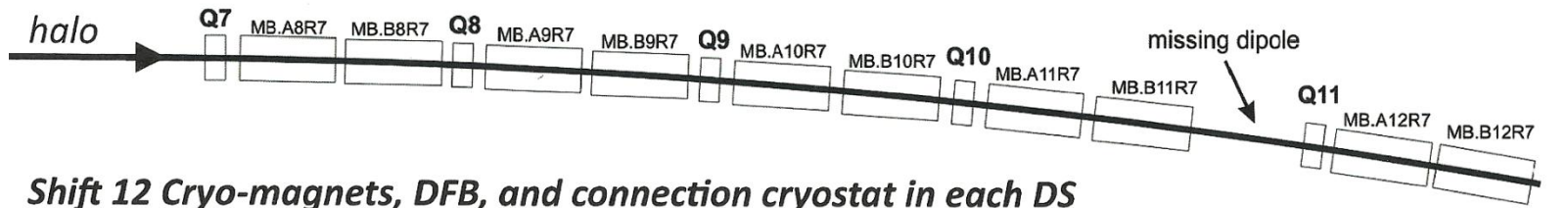
RB output voltage: ± 10 V

(-)

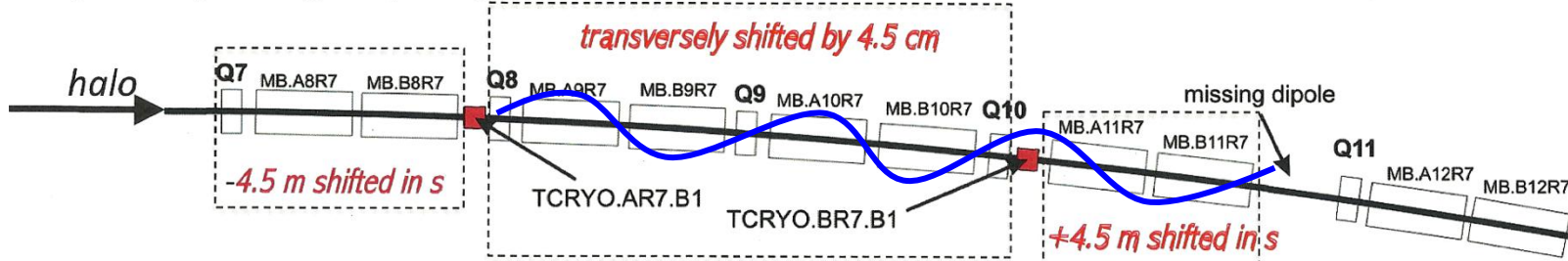
- Protection of the magnets
- Floating Trim PCs (> 2 kV)
- coupled circuits

non-local correction: dedicated MCBH in an free part of the lattice
does not change the picture: there will always be a **inner orbit distortion**
 in the order of several mm ... the only question is how localised
 we can keep the problem

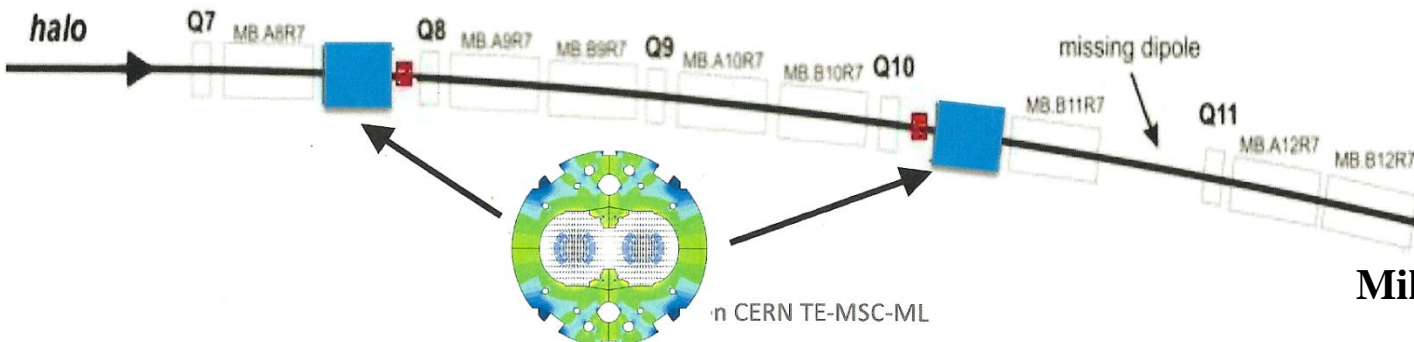
DS Upgrade Scenarios



Shift 12 Cryo-magnets, DFB, and connection cryostat in each DS



New 3..3.5 m shorter Nb3Sn Dipoles (2 per DS)



Mikko Karppinen

5.) Nb3Sn Dipole: Multipole Errors:

Systematic errors

Current

(A)	B1	b2	b3	b4	b5	b6	b7
763	-0.7325	2.50	13.96	0.02	-0.24	0.00	0.29
1456	-1.3977	2.50	13.96	0.02	-0.24	0.00	0.29
2149	-2.0628	2.50	13.96	0.02	-0.24	0.00	0.29
2842	-2.7279	2.50	13.96	0.02	-0.24	0.00	0.29
3535	-3.3930	2.50	13.96	0.02	-0.24	0.00	0.29
4228	-4.0581	2.49	13.96	0.02	-0.24	0.00	0.29
4921	-4.7231	2.48	13.97	0.02	-0.24	0.00	0.29
5614	-5.3875	2.45	13.99	0.02	-0.23	0.00	0.29
6307	-6.0499	2.28	14.03	0.01	-0.23	0.00	0.29
7000	-6.7075	1.84	14.15	-0.01	-0.23	0.00	0.29
7692	-7.3565	1.05	14.31	-0.04	-0.21	0.00	0.29
8385	-7.9928	-0.21	14.36	-0.10	-0.18	0.00	0.29
9078	-8.6120	-2.13	14.21	-0.21	-0.17	-0.01	0.29
9771	-9.2204	-4.43	13.97	-0.31	-0.15	-0.01	0.29
10464	-9.8212	-6.94	13.68	-0.41	-0.14	-0.02	0.29
11157	-10.4160	-9.68	13.37	-0.51	-0.13	-0.02	0.30
11850	-11.0060	-12.49	13.06	-0.58	-0.13	-0.02	0.30

... in the usual units, i.e. 10^{-4} referred to the usual ref radius = 17mm

Nb3Sn Dipole: Multipole Errors:

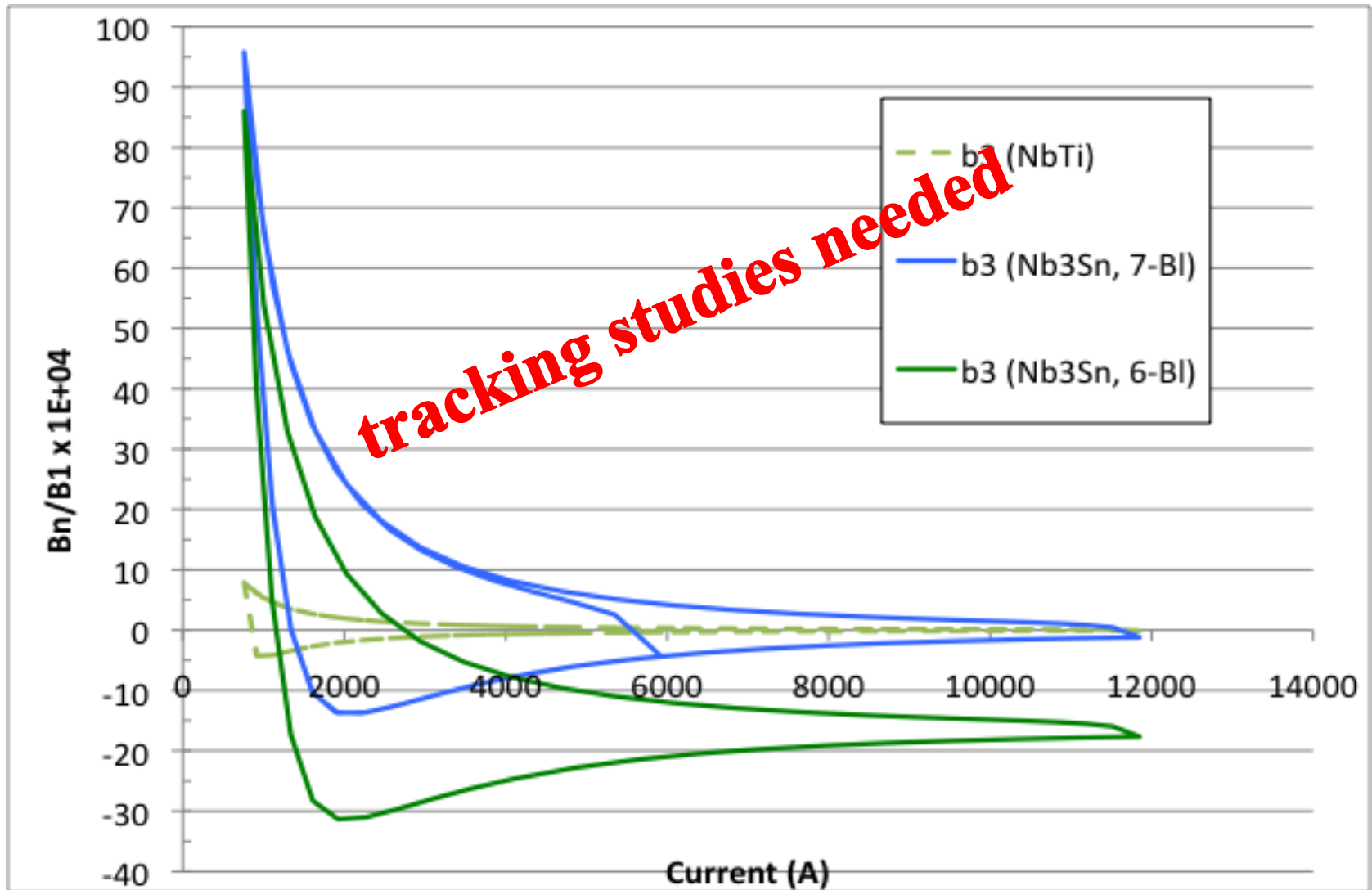
Persistent current analysis Nb3Sn Dipole				
Current (A)	TF (T/A)	B1 (T m)	b3 (Units)	b5 (Units)
758	-9.68E-04	-7.92E+00	9.58E+01	-1.34E+00
911	-9.60E-04	-9.45E+00	5.36E+01	1.58E+00
1105	-9.54E-04	-1.14E+01	2.12E+01	3.33E+00
1337	-9.50E-04	-1.37E+01	2.31E-01	3.80E+00
1610	-9.48E-04	-1.65E+01	-1.05E+01	3.23E+00
1923	-9.47E-04	-1.97E+01	-1.37E+01	2.19E+00
2276	-9.47E-04	-2.33E+01	-1.36E+01	1.35E+00
2668	-9.47E-04	-2.73E+01	-1.24E+01	7.94E-01
3101	-9.48E-04	-3.17E+01	-1.09E+01	4.52E-01
3573	-9.48E-04	-3.66E+01	-9.27E+00	2.47E-01
4086	-9.48E-04	-4.18E+01	-7.76E+00	1.28E-01
4862	-9.49E-04	-4.98E+01	-5.99E+00	4.25E-02
5639	-9.49E-04	-5.78E+01	-4.72E+00	9.44E-03
6415	-9.49E-04	-6.57E+01	-3.80E+00	-2.50E-03
7192	-9.49E-04	-7.37E+01	-3.11E+00	-5.54E-03
7968	-9.49E-04	-8.17E+01	-2.58E+00	-4.68E-03
8744	-9.49E-04	-8.96E+01	-2.17E+00	-2.09E-03
9521	-9.49E-04	-9.76E+01	-1.84E+00	1.21E-03
10297	-9.49E-04	-1.06E+02	-1.58E+00	4.74E-03
11074	-9.49E-04	-1.14E+02	-1.36E+00	8.27E-03
11850	-9.49E-04	-1.22E+02	-1.18E+00	1.17E-02
11517	-9.50E-04	-1.18E+02	4.44E-01	1.38E-03

NbTi Dipole: Multipole Errors:

For comparison the same data for the **NbTi MB** coil in the same co

Current (A)	TF (T/A), Nb	TF (NbTi)	b3 (NbTi)	b5 (NbTi)
758	-7.17E-04	-7.78E+00	7.89E+00	-7.39E-01
911	-7.16E-04	-9.34E+00	-4.26E+00	9.21E-01
1105	-7.16E-04	-1.13E+01	-4.18E+00	5.23E-01
1337	-7.16E-04	-1.37E+01	-3.45E+00	3.36E-01
1610	-7.16E-04	-1.65E+01	-2.68E+00	2.39E-01
1923	-7.16E-04	-1.97E+01	-2.07E+00	1.78E-01
2276	-7.17E-04	-2.33E+01	-1.61E+00	1.35E-01
2668	-7.17E-04	-2.73E+01	-1.27E+00	1.04E-01
3101	-7.17E-04	-3.18E+01	-1.01E+00	8.06E-02
3573	-7.17E-04	-3.66E+01	-8.08E-01	6.31E-02
4086	-7.17E-04	-4.19E+01	-6.55E-01	4.96E-02
4862	-7.17E-04	-4.98E+01	-4.96E-01	3.58E-02
5639	-7.17E-04	-5.78E+01	-3.89E-01	2.67E-02
6415	-7.17E-04	-6.57E+01	-3.14E-01	2.02E-02
7192	-7.17E-04	-7.37E+01	-2.59E-01	1.55E-02
7968	-7.17E-04	-8.17E+01	-2.16E-01	1.19E-02
8744	-7.17E-04	-8.96E+01	-1.83E-01	9.14E-03
9521	-7.17E-04	-9.76E+01	-1.57E-01	6.93E-03
10297	-7.17E-04	-1.06E+02	-1.35E-01	5.15E-03
11074	-7.17E-04	-1.13E+02	-1.17E-01	3.69E-03
11850	-7.17E-04	-1.21E+02	-1.03E-01	2.48E-03

the persistent current problem:



11T Dipole Project

1. **Project definition** (Sep '10-Feb '11)
 - Schedule
 - Responsibilities and contributions, available resources
 - Funding
2. **Study phase** (Sep '10-Mar '11)
 - Impact on the LHC
 - Definition of the parameters and boundary conditions
 - Conceptual design
3. **D&D-phase** (Mar '11-Dec '13)
 - Magnet design
 - Supporting studies
 - Model Program
 - *Go/No-Go Decision* (Jan '13)
4. **Production phase** (Jun '13-Dec '16)

Resume: Nb₃Sn dipoles in the cold collimation part

have (nearly) **no effect on the beam optic**

have (nearly) **no effect on the LHC global geometry**
local geometry has to be discussed

have a strong influence on the orbit that can be
corrected outside the dipole pair
using a considerable fraction of the available
corrector strength

a relatively large orbit distortion (5σ) remains
between the dipole pairs

would be a great idea to **install trim power supply** to compensate
the effect and forget about the problems !!!

multipoles are enormous and have to be studied
for injection energy, flat top, 3.5 TeV ??