

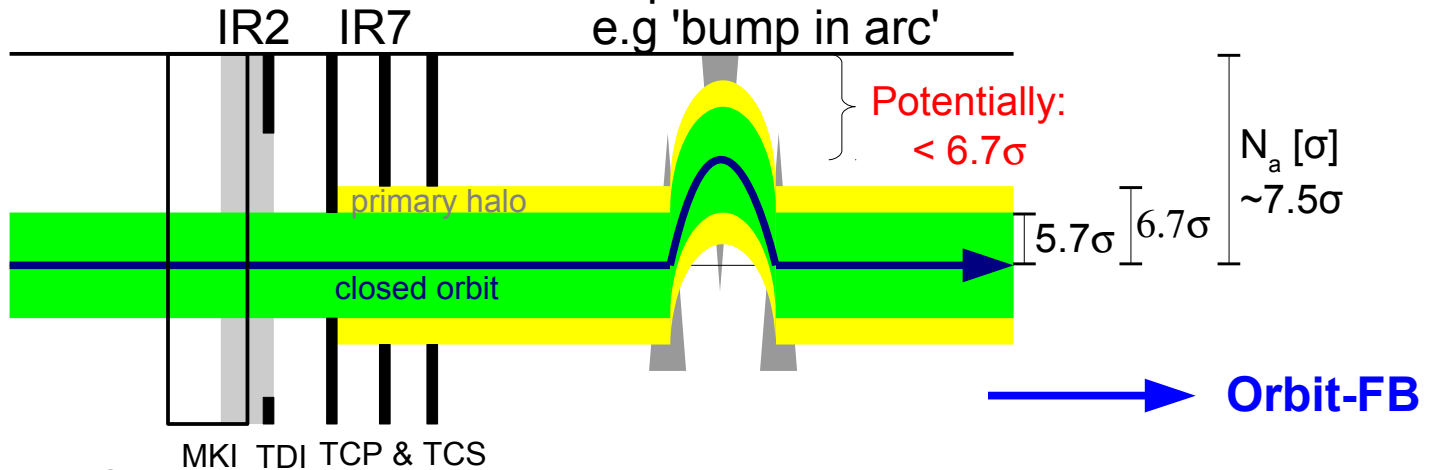
Some Notes on:

Continuous LHC Beta-Beat Measurements – Status and Prospects for 2011 –

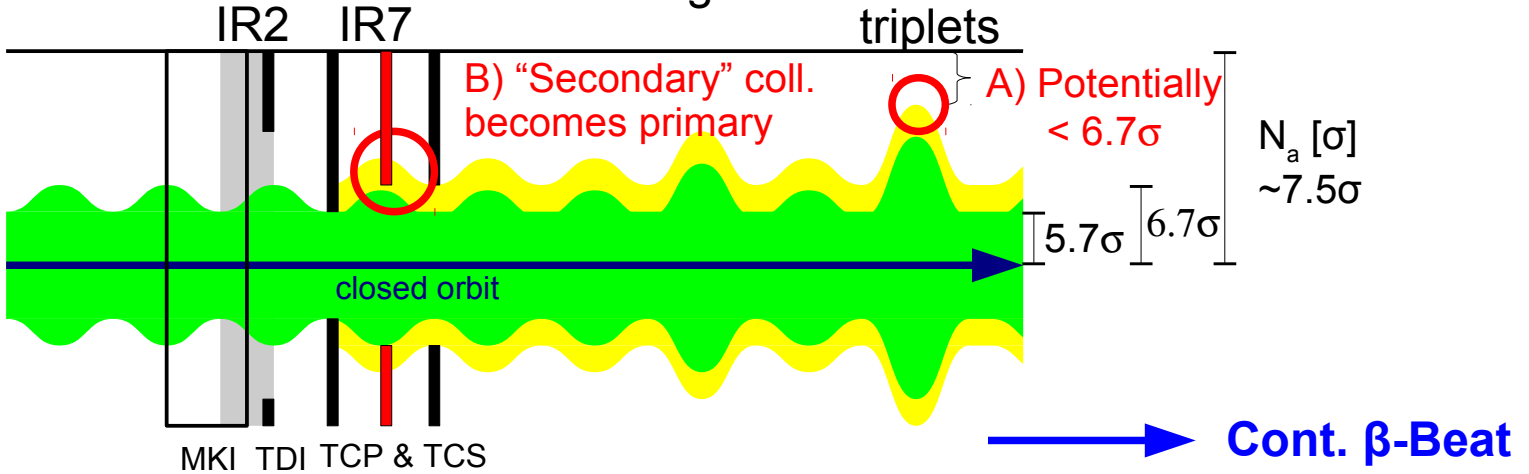
R. J. Steinhagen, A. Boccardi, E. Calvo Giraldo,
M. Gasior, J. L. Gonzalez, O. R. Jones, BE-BI

- Motivation – LHC dependence on known & constant beta-function
 - Machine Protection and Collimation, Physics, Squeeze Diagnostics
 - various existing techniques: 'kick'-type excitation & BPMs, K-modulation & Q-PLL, Closed-orbit-response (LOCO)
 - do not achieve required resolution, and/or
 - not compatible with nominal LHC operation (ex. levels/beam intensities)
- The aim of the continuous beta-beat measurement studies at the LHC was to
 - provide a proof-of-feasibility for the measurement technique, and
 - to assess magnitude and time-scale of the LHC lattice changes.
- Continuous Beta-Beat system working principle
 - difference to BPM-based acquisition
 - Fundamental constraints and limits
 - LHC installation
- Some examples taken at the SPS and LHC

- Combined failure and local orbit bumps:



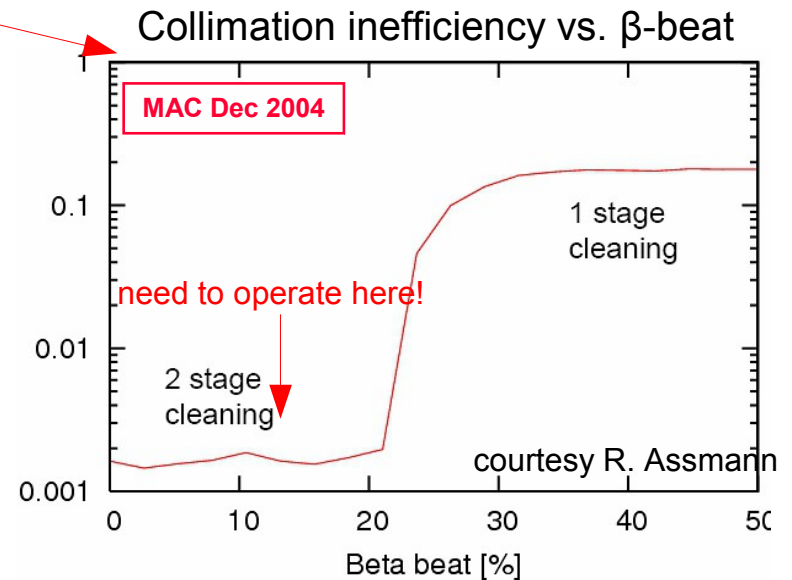
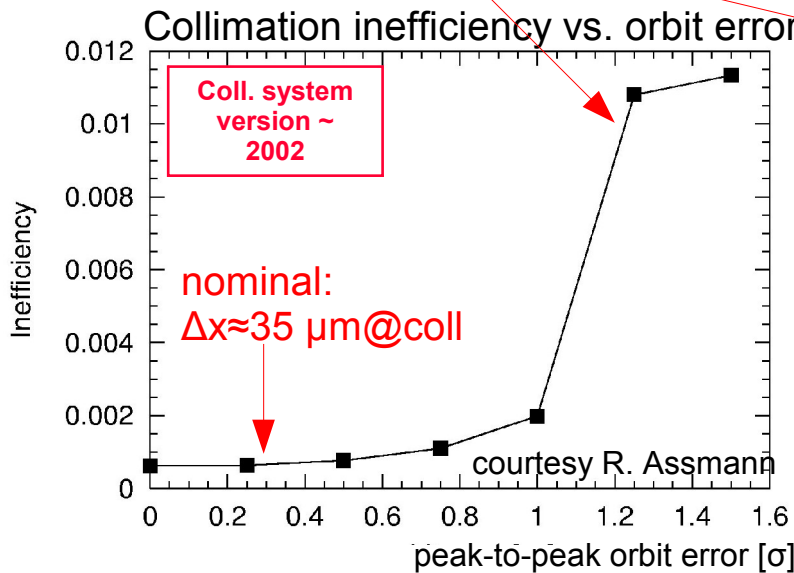
- Combined failure and local beta-beating:



- Limits maximum safe intensity and minimum β^* in the LHC
 - Mitigation: tighter collimator settings (but implies less aperture \rightarrow poorer life-time)

- Two beta-beat components:
 - Static-global → AC-dipole driven + BPMs (R. Tomas et al.)
 - absorbed by the beam-based collimator alignment procedure
 - Dynamic-local → continuous beta-beat system (BI, IPAC'10)
 - check whether these requirements are kept in a fully dynamic case
 - initial installation around the primary collimators in IR7

$$N_{max} \leq \frac{\tau_{min} \cdot R_q \cdot L_{dil.}}{\eta} \longrightarrow L_{max} \approx \frac{1}{4\pi} \cdot \frac{N_{max} \cdot n_b \cdot f_{rev}}{\beta^* \epsilon}$$



- Nominal collimator settings also imply maximum μm -level beam excursions before scraping the beam

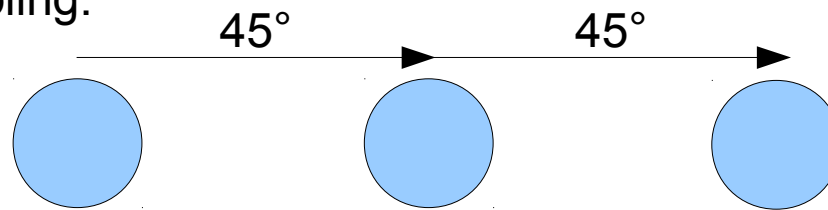
- Squeeze involves > 45 individual magnetic strength settings (Optics), so far: no continuous check on effective optics during/at the end of individual steps
- “Classic” methods may not reach/be compatible with nominal requirements
 - K-modulation induced Q-Changes:
$$\Delta Q \approx \frac{1}{4\pi} \cdot \beta(s) \cdot \Delta k(s)$$
 - Limit: knowledge on quadrupole transfer function (hysteresis, D&S, $\beta|^{max} \approx 4.2\text{km}$ & $\Delta Q^{max} < 10^{-3} \rightarrow \Delta k/k_{nom} < 5 \cdot 10^{-5}$)
 - Betatron-coupling, ...
 - Only local (& slow) measurement
 - Kick + turn-by-turn analysis of BPM (phase and/or amplitude), limits:
 - Potential particle loss (beta-functions at triplet) & emittance blow-up
 - Systematic phase errors, amplitude detuning/Landau damping
 - large kicks may probe phase advances (dynamic aperture) which may not be representative for nominal beam operation
 - beam will be collimated at 6 sigma (kick amplitudes < 1.2 mm @7TeV)!
 - ... not ideal for continuous monitoring/regular operation (ϵ blow-up).
 - Closed orbit response analysis (LOCO):
 - resolution/performance compatible with nominal operation
 - Limit: scan requires several minutes per IP (full scan: ~2 OP-shifts)

- Long history at CERN. Original idea dates back to AB-BI report (doctoral thesis) P.Castro, *Luminosity and Betatron Function Measurement at [...] LEP*, CERN SL/96-70 (BI)
- ... beating in amplitude related to **beating in phase**:

$$\frac{\Delta\beta}{\beta}(s) = \frac{1}{2 \sin(2\pi Q)} \oint \beta_k \cos(2 \cdot |\mu(s) - \mu(a)| - 2\pi Q) \Delta k(a) da$$

$$\mu(s) := \int_0^s \frac{1}{\beta(a)} da \quad \longrightarrow \quad \frac{\Delta\mu}{\mu}(s) \sim \frac{\Delta\beta}{\beta}(s)$$

- Phase sampling:



Case I: $\Delta\phi$ (blue arrow pointing right) 0 $-\Delta\phi$ (blue arrow pointing left) $\Delta\mu_{12} = 45^\circ - \Delta\phi$, $\Delta\mu_{13} = 90^\circ - 2\Delta\phi$

Case II: 0 $\Delta\phi$ (red arrow pointing right) 0 $\Delta\mu_{12} = 45^\circ + \Delta\phi$, $\Delta\mu_{13} = 90^\circ$

- Beta-Beat reconstruction (FB/Control would work with phases):

$$\frac{\Delta\beta_1}{\beta_1} = \frac{\cot(\Delta\mu_{12}^{meas.}) - \cot(\Delta\mu_{13}^{meas.})}{\cot(\Delta\mu_{12}^{theo.}) - \cot(\Delta\mu_{13}^{theo.})} \quad \frac{\Delta\beta_2}{\beta_2} = \frac{\cot(\Delta\mu_{12}^{meas.}) - \cot(\Delta\mu_{23}^{meas.})}{\cot(\Delta\mu_{12}^{theo.}) - \cot(\Delta\mu_{23}^{theo.})} \quad \frac{\Delta\beta_3}{\beta_3} = \frac{\cot(\Delta\mu_{23}^{meas.}) - \cot(\Delta\mu_{13}^{meas.})}{\cot(\Delta\mu_{23}^{theo.}) - \cot(\Delta\mu_{13}^{theo.})}$$

N.B. Phase-Beating usually used for correction!

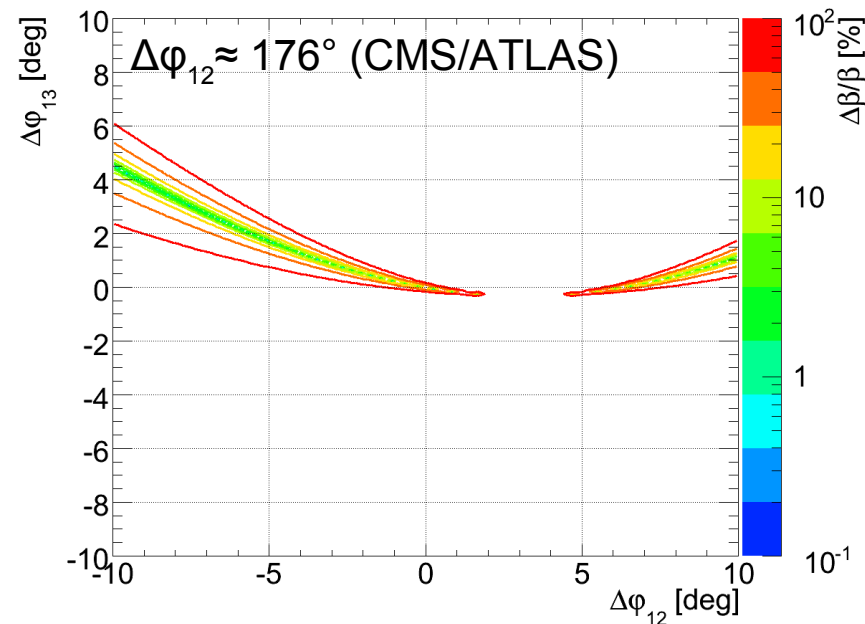
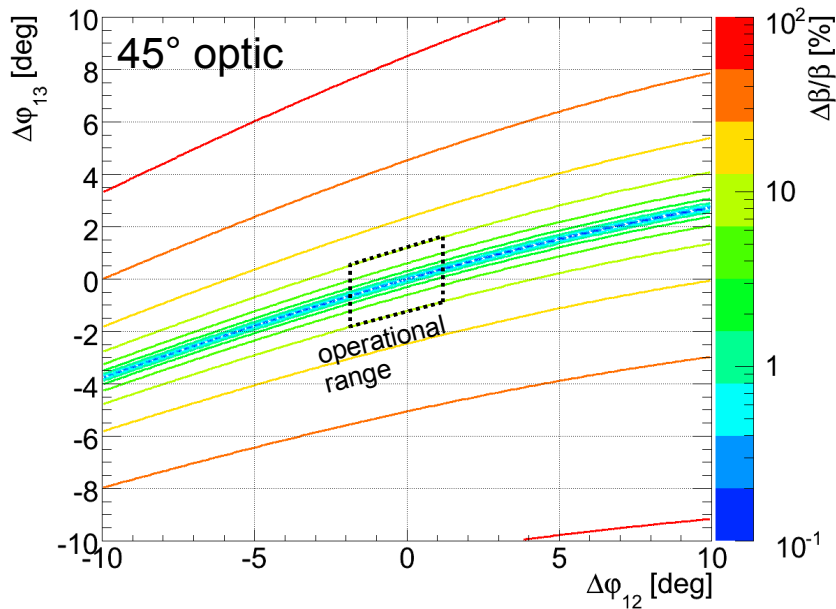
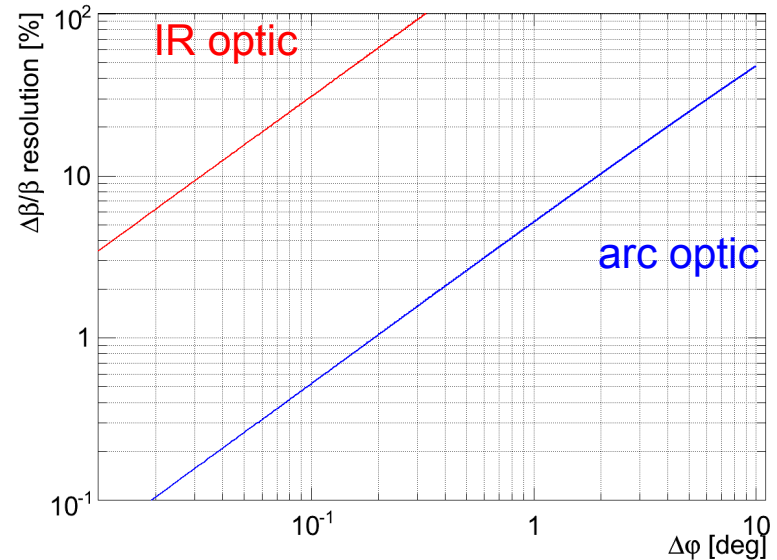
Residual resolution/systematic error

$$\frac{\Delta \beta_1}{\beta_1} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

$$\Delta \mu_{1i}^{meas.} := \Delta \mu_{1i}^{theo.} + \Delta \varphi_{1i}$$

- ARC optics: requires error below $\sim 1^\circ$
- IP optics: requires error below $\sim 0.02^\circ$

N.B. Plots have logarithmic z-scale!



Beta-Beat Measurement Error Sources I/II

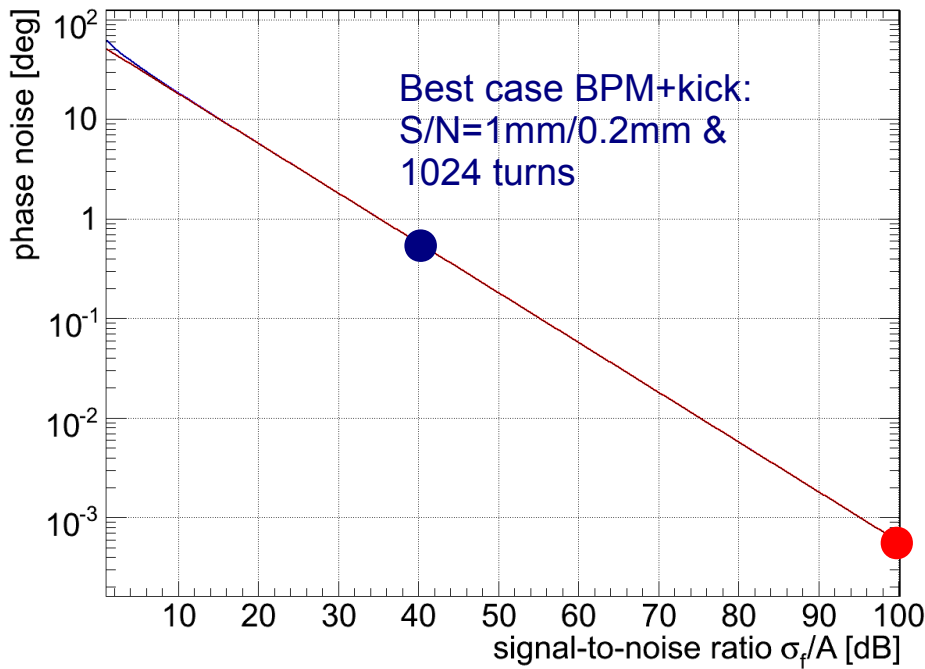
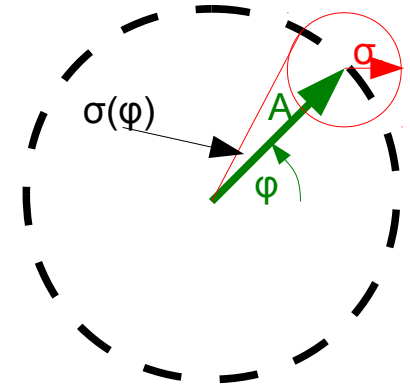
Statistical Phase Noise

- Statistical noise adds vectorial to the carrier signal:

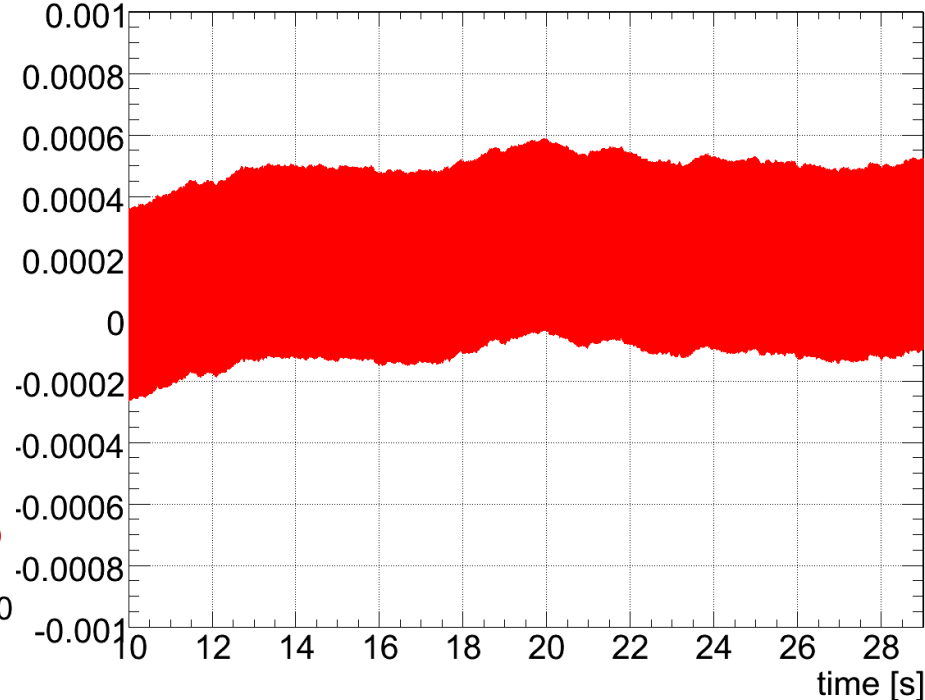
- excitation amplitude (carrier signal): A
- noise in time (frequency) domain: σ_t (σ_f)
- Equivalent number of turns: N

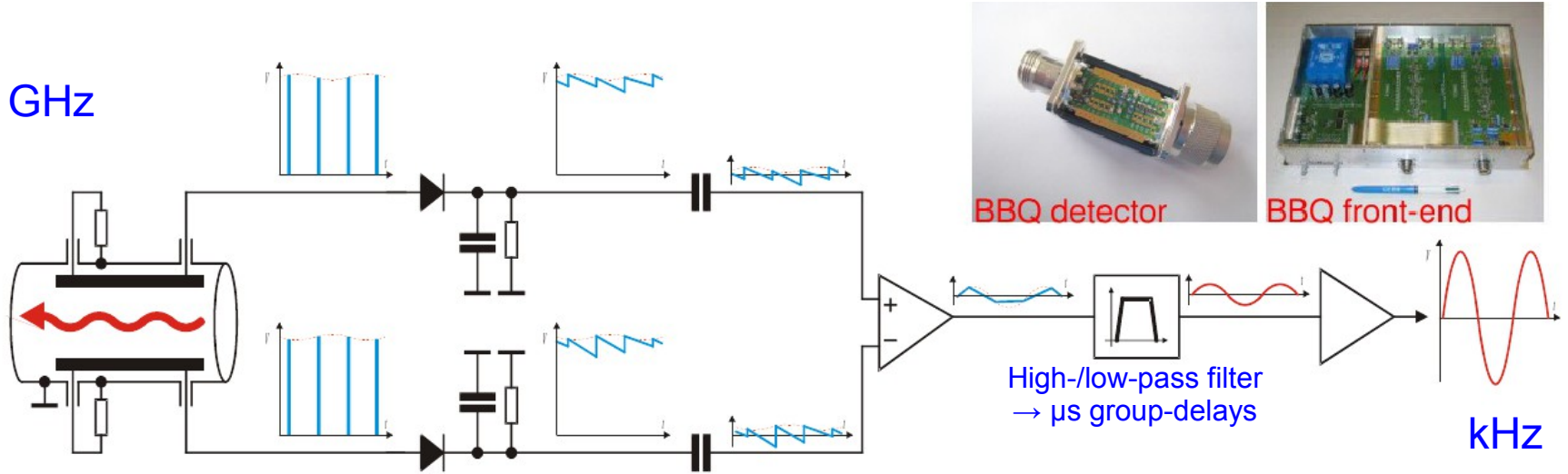
$$\sigma(\varphi) = \arcsin\left(\frac{\sigma_f}{A}\right) = \arcsin\left(\sqrt{\frac{2}{N}} \frac{\sigma_t}{A}\right)$$

for small noise to signal ratios $\approx \sqrt{\frac{2}{N}} \frac{\sigma_t}{A}$



Delta 1010 intrinsic phase noise@1Hz



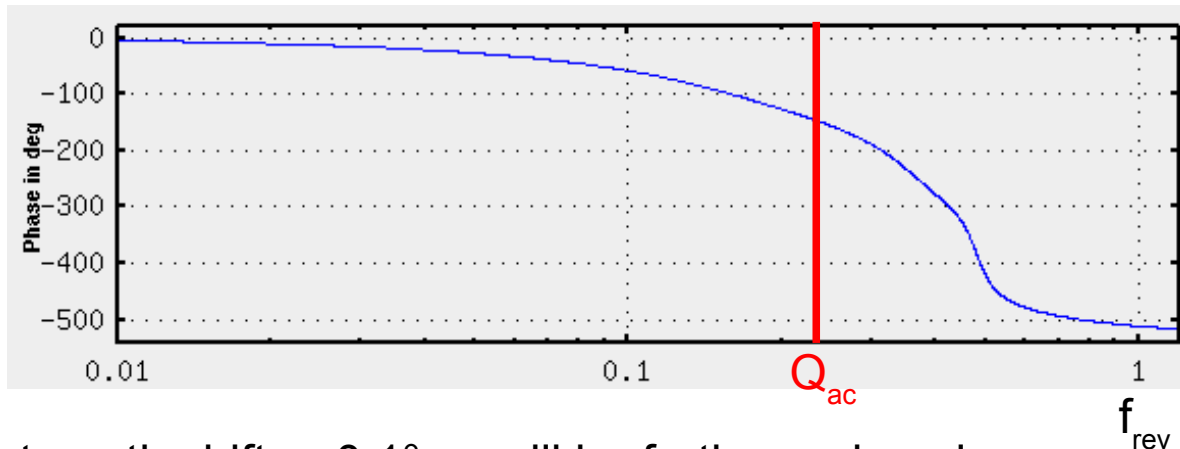


- **Basic principle: AC-coupled peak detector¹**
 - intrinsically down samples beam spectra: GHz \rightarrow kHz ('Base-Band-Tune Meter')
 - Base-band operation: very high sensitivity < 10 nm/turn \rightarrow ϵ blow-up is a non-issue
 - AC-coupling removes common-mode \rightarrow only relative changes play a role
 - capacitance keeps the “memory” of the to be rejected signal
 - robust: no saturation, self-triggered, no gain changes to accommodate single vs. multiple bunches or low vs. high intensity beam

- **However: BBQ \neq Beam Position Monitor**
 - Fundamentally different acq. techniques but yielding same 'phase-advance information)
 - (Analogue: TF measurement using step generator and scope vs. network analyser)

¹M. Gasior, “The principle and first results of betatron tune measurement by direct diode detection”, CERN-LHC-Project-Report-853, 2005

- Sources – usually depend on observation/excitation frequency
 - Systematic delays: $\Delta\varphi [deg] = 360^\circ \cdot \Delta\tau f$
 - Pick-up to acquisition system cable length (e.g. 100 m @ $Q_{AC} = 0.25 f_{rev}$)
 - SPS: $\Delta\varphi \approx 2^\circ$ LHC $\Delta\varphi \approx 0.5^\circ$: $\Delta\beta/\beta_{sys.} \approx 3-10\%$ (45° lattice)
 - However, is suppressed for relative beta-beat measurements
 - Low-frequency pre-processing and analogue front-end asymmetry (mostly HP/LP-filters $\rightarrow \mu s$ -level group delays)
 - Delta 1010 – analogue pre-filter: $\Delta\varphi \approx 7^\circ$ (measured)
 - BBQ front-end: $\Delta\varphi \approx 10^\circ$ (measured, here: only Chebychev stage shown)

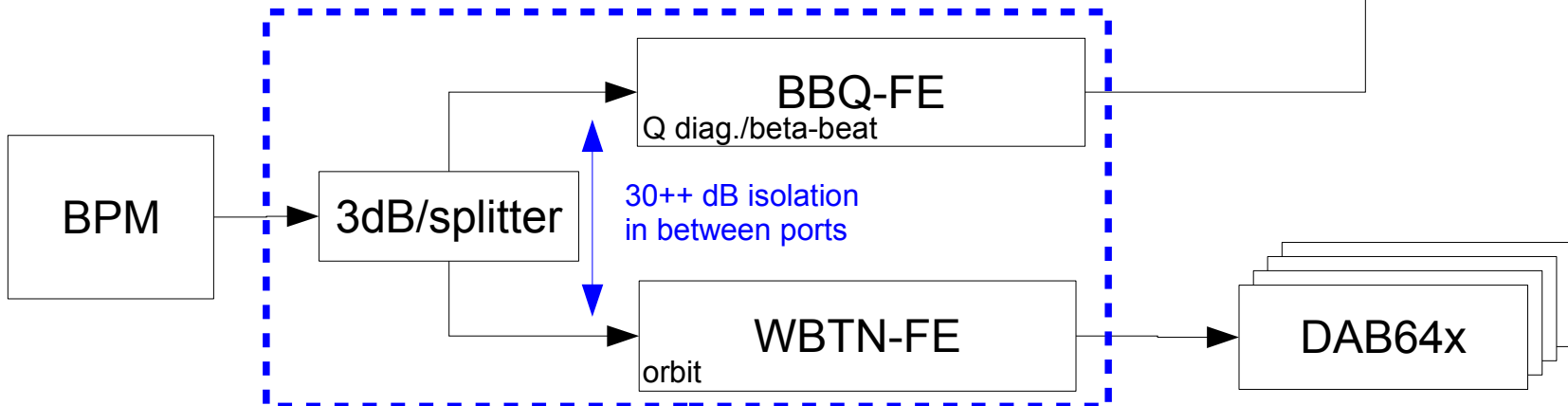


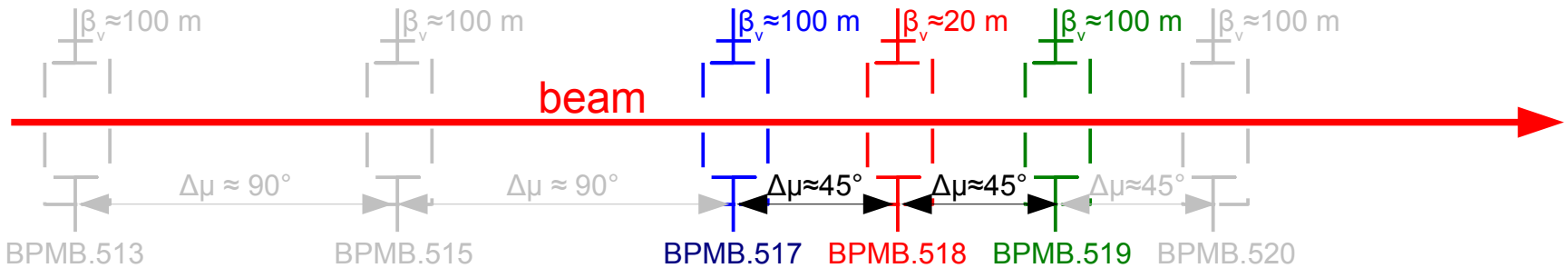
- Systematic drift: $< 0.1^\circ \rightarrow$ will be further reduced

- KISS digital acquisition: HP Proliant 16", 1U + M-AUDIO Delta 1010
 - 8 analogue inputs/outputs, 16", 1U
 - frequency response: 20Hz-22kHz, +/-0.3dB
 - >100 dB dynamic range/S/N ratio
 - THD: 0.00072% (A/D), 0.00200% (D/A)
 - N.B. til-date: no single-event upsets despite being next to the primary B1 collimators

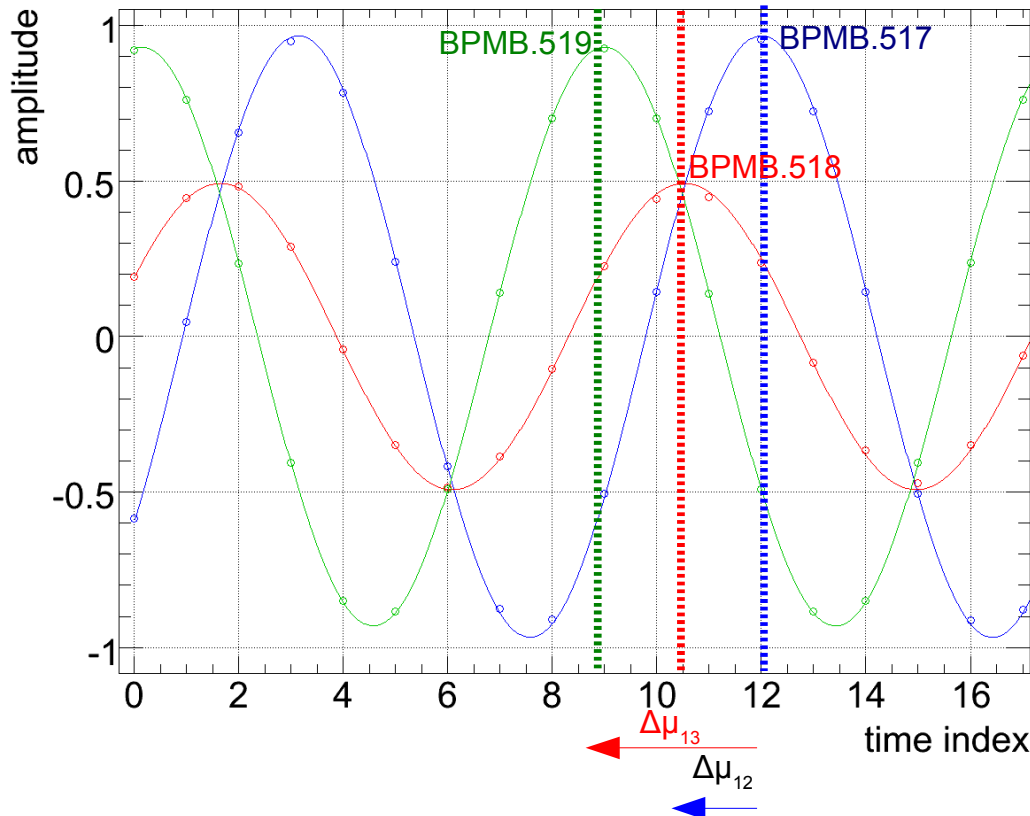
allows simple filtering and post-processing in audio domain

- Tests with beam in the SPS & LHC confirm that there is no obvious cross-talk in between the regular LHC WBTN (orbit) and the diode-based continuous beta-beat acquisition electronics.





■ Measurement (markers), sinusoidal fit (solid line):

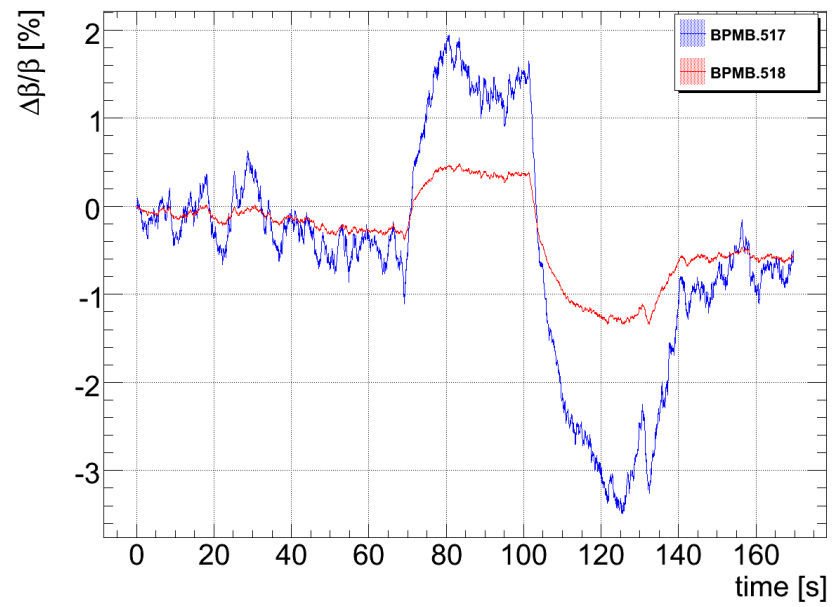
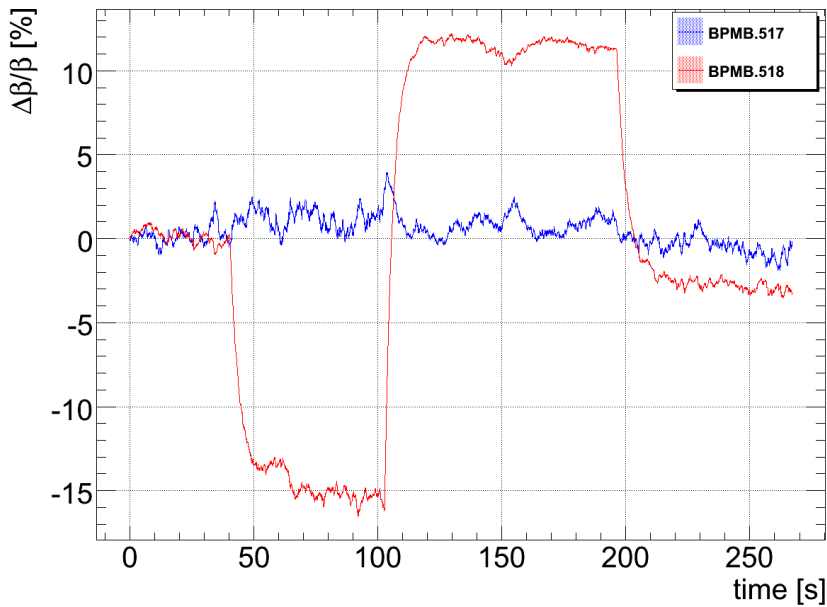
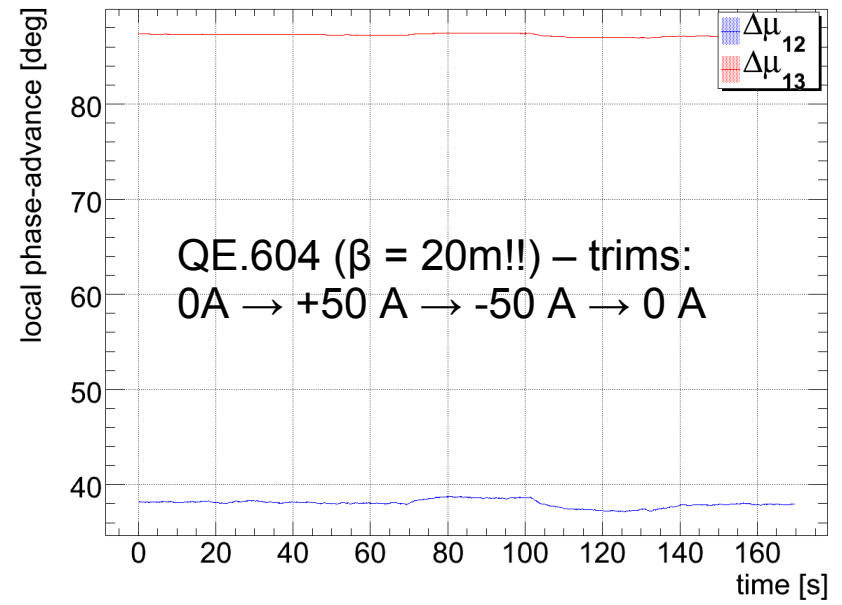
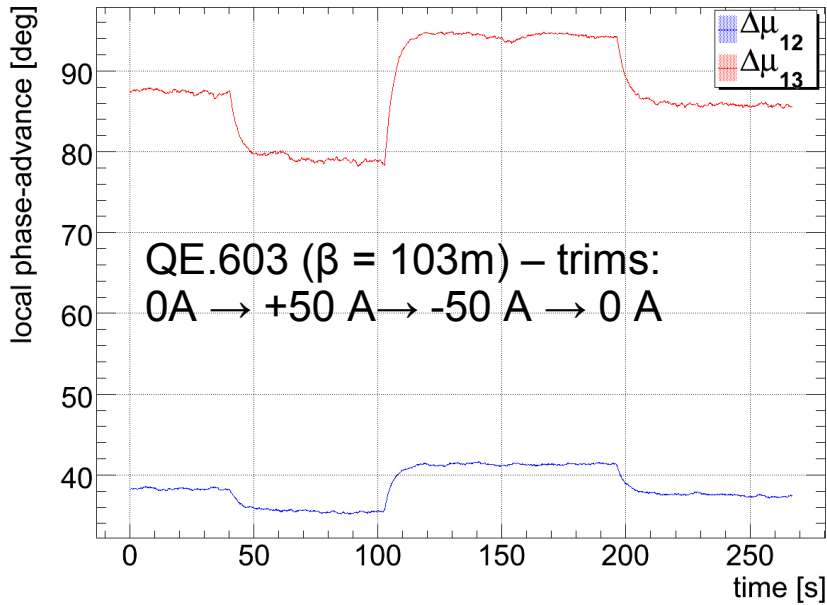


$$\frac{\Delta \beta_1}{\beta_1} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

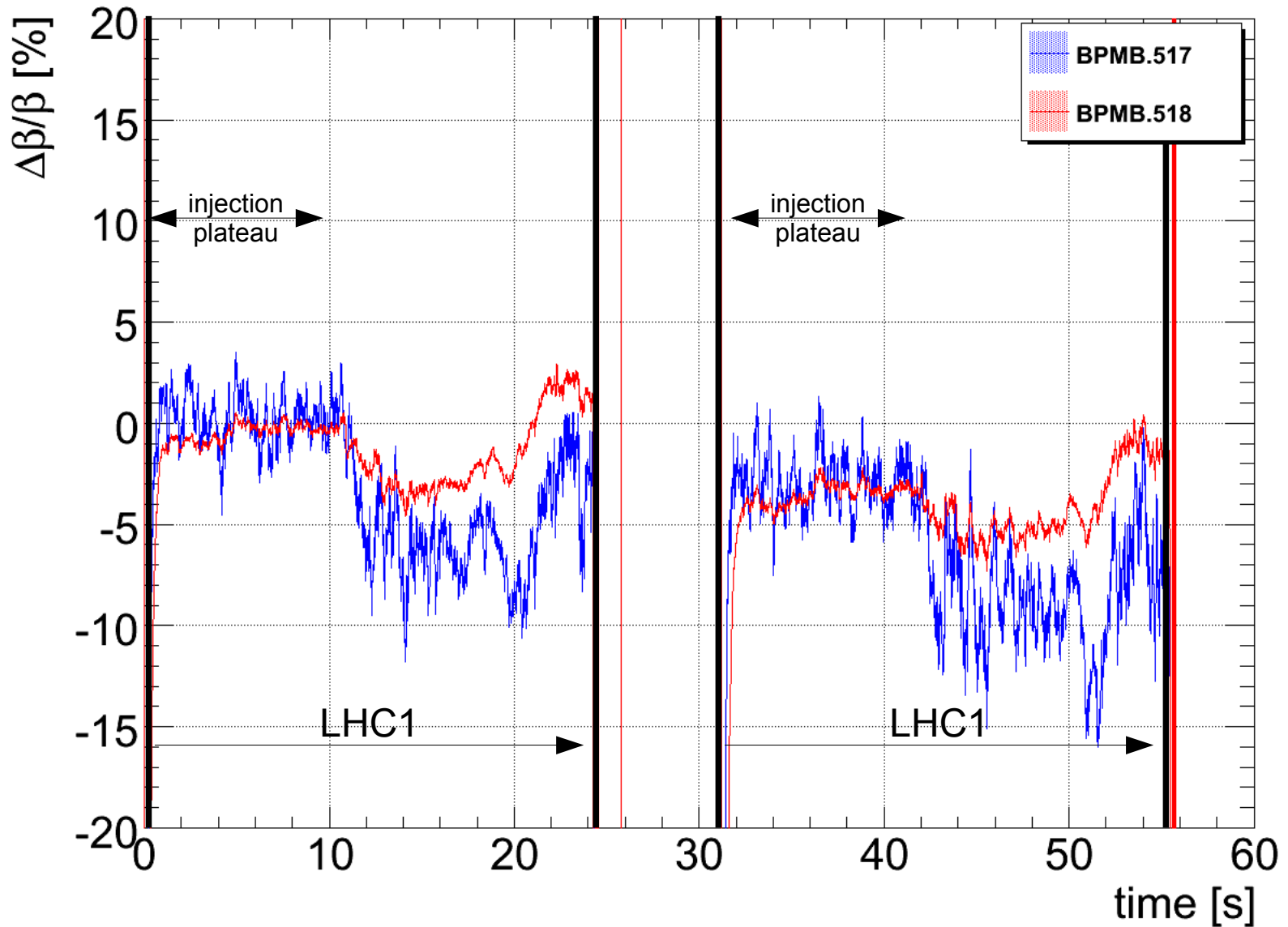
$$\frac{\Delta \beta_2}{\beta_2} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{23}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{23}^{theo.})}$$

$$\frac{\Delta \beta_3}{\beta_3} = \frac{\cot(\Delta \mu_{23}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{23}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

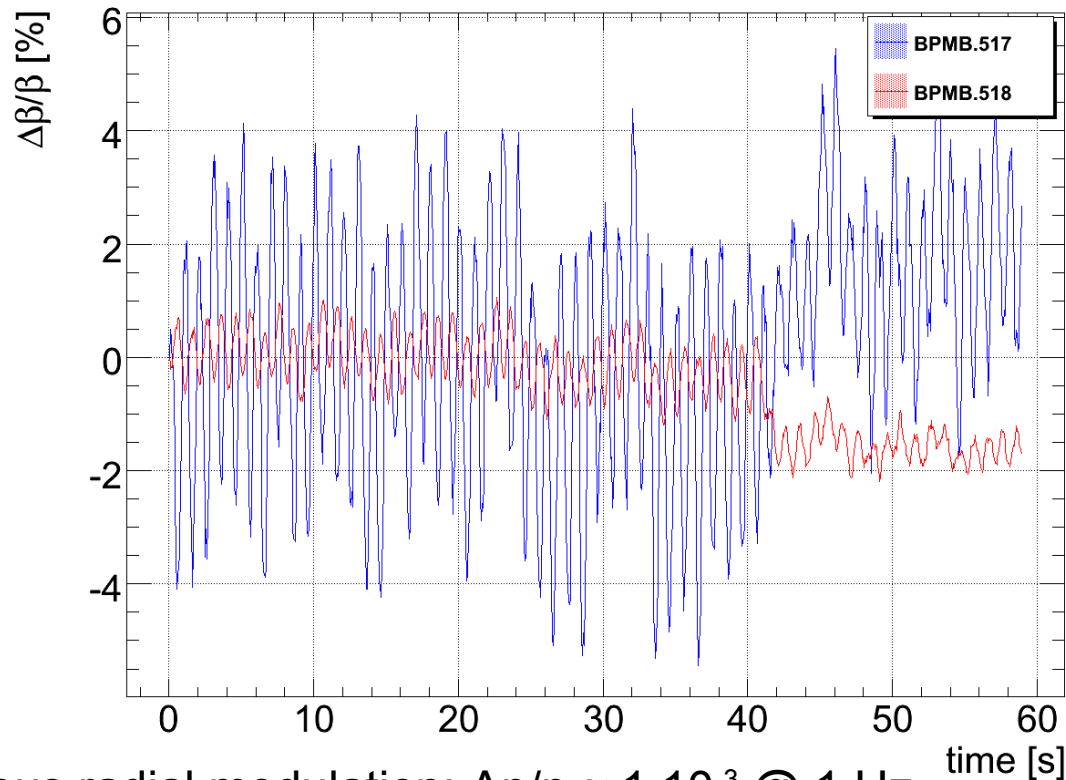
QE.603/QE.604 induced β -Phase-Advance Beating



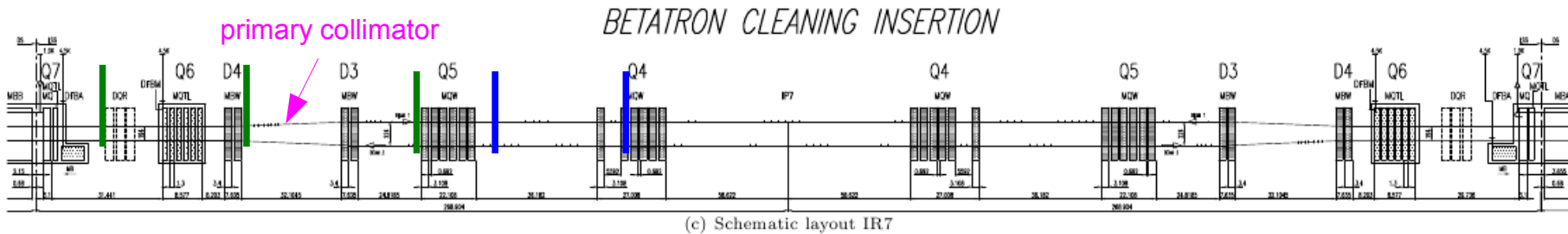
- In between two coasts...



- System can be further exploited for fast and transparent measurements of physics affecting $\Delta\beta/\beta$ that earlier required significant amount of beam time
- Example: vertical off-momentum β -Beat:



- Continuous radial modulation: $\Delta p/p \approx 1 \cdot 10^{-3} @ 1 \text{ Hz}$
- One full measurement data set every second!
- N.B. Step in phase \rightarrow off-centre horizontal orbit in lattice sextupoles

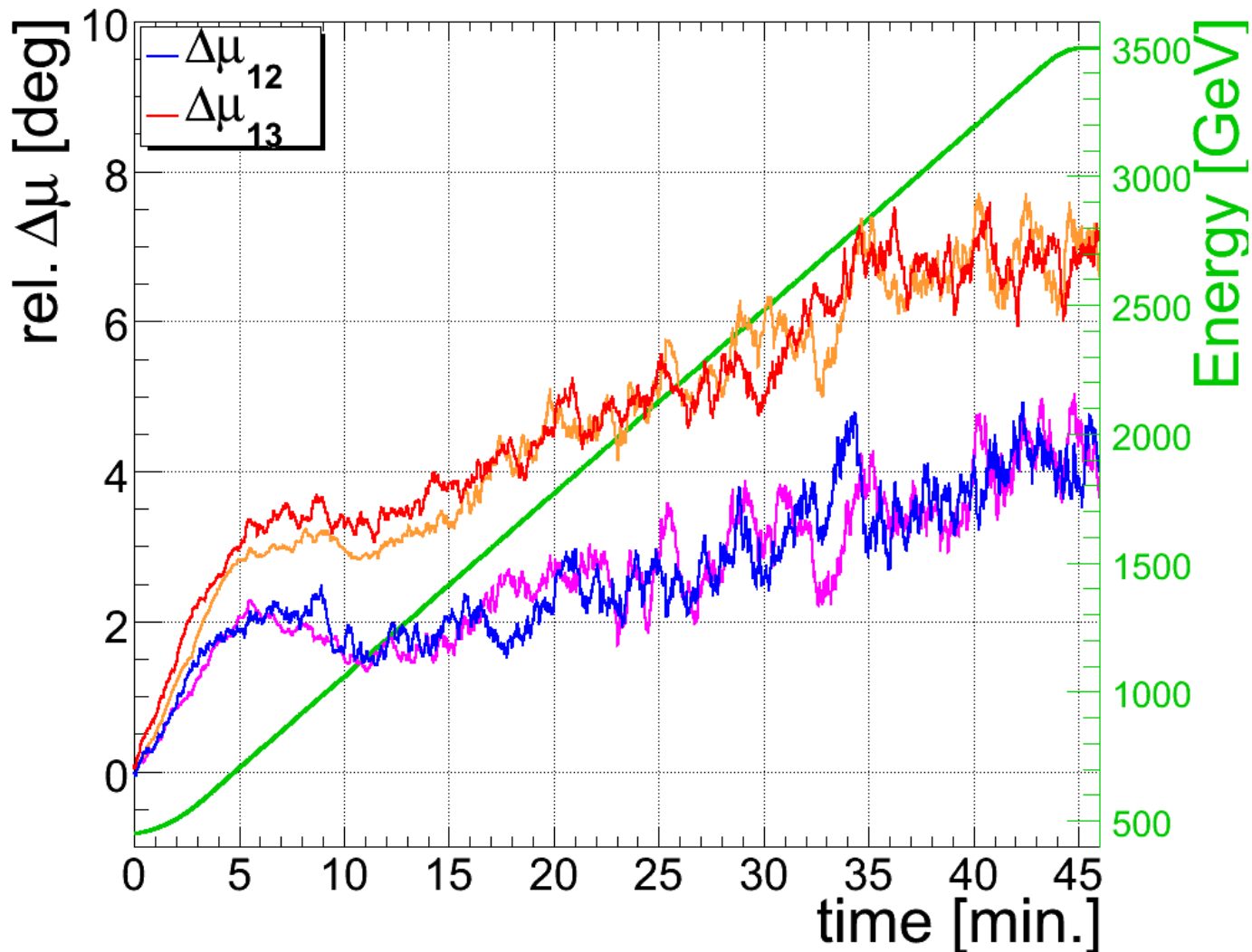


- Located in RR73, the minimum installation without pulling additional cables
- Pick-ups: BPM.7L7.B1 → BPMWC.6L7.B1 → BPMW.5L7.B1
 - phase-advance in between of $\Delta\mu \approx 45^\circ$
 - dual-plane → 6 channels
- Present installation using 3dB-Splitters works fine for a few (<6-8) pick-up locations but does not scale well (costs) for massive deployment (dominated by HF cabling, connector, mechanics, etc...)
 - Re-used default BBQ front-ends (not optimised for phase stability)
 - Non-issue for relative beta-beat change measurements
 - Was/can be cross-calibrated (once) against standard BPMs

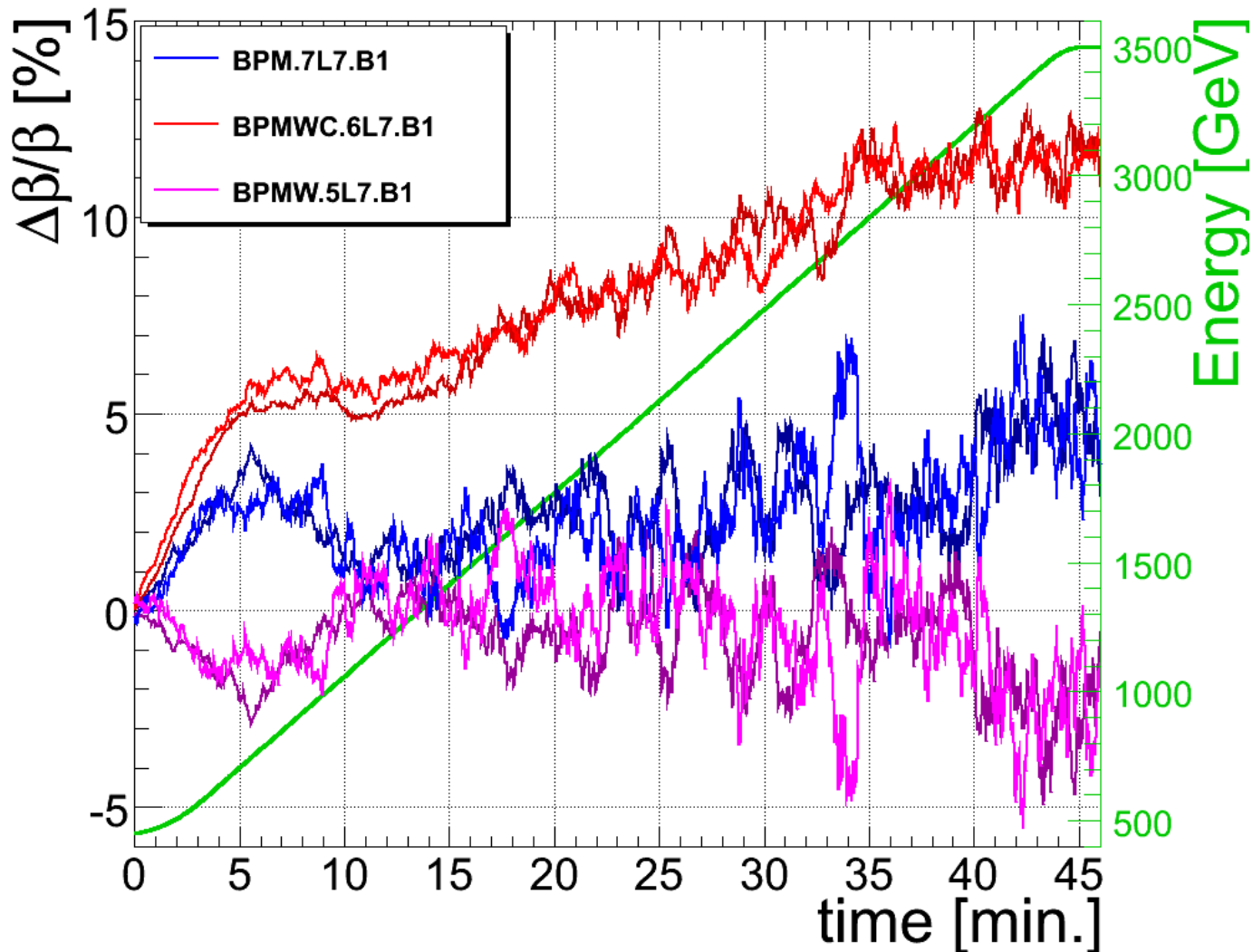
LHC Beta-Beat during the Energy Ramp I/III

– Raw BPM-to-BPM phase-advance measurement

- Perfectly pre-cycled machine, off-resonance excitation, $< \mu\text{m}$ excitation level
 - excellent phase resolution, reduces with energy (N.B. const. kick strength)



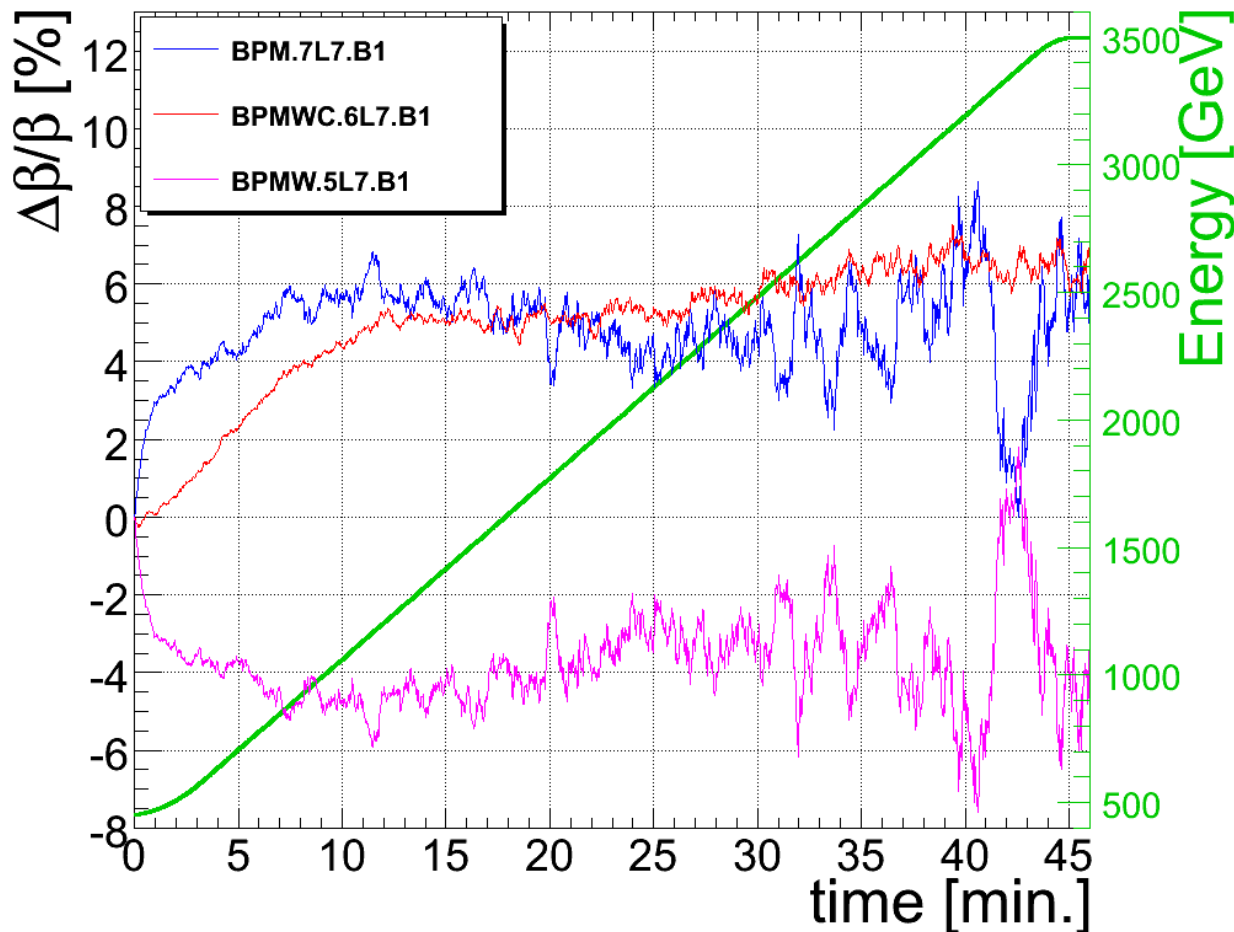
LHC Beta-Beat during the Energy Ramp II/III – Reconstructed Local Beta-Beat



- Excellent fill-to-fill reproducibility of about 1% – provided machine underwent a standard magnetic pre-cycle and no quenches have occurred.
- Complemented also by Rogelio's reproducibility assessment

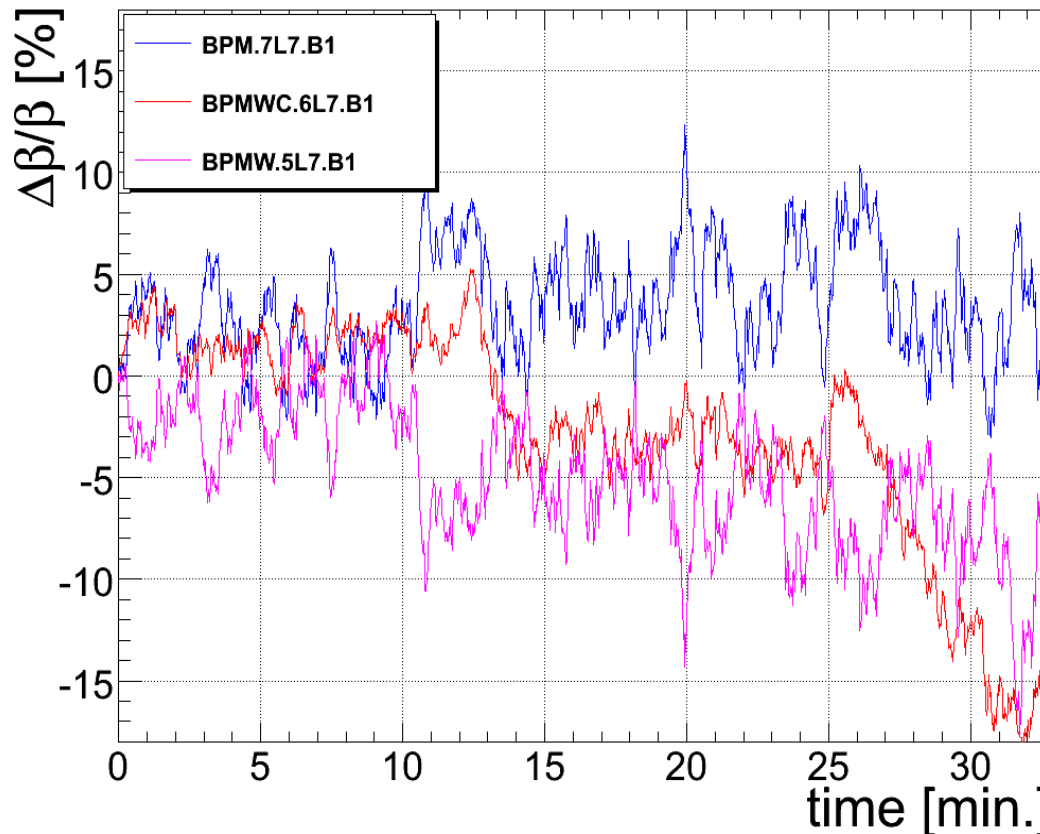
LHC Beta-Beat during the Energy Ramp III/III – Evolution during a “less-perfect” Ramp

- 3/8 main dipole circuits being pre-cycled to 2 kA instead of the default 6 kA.
- Percent-level correction of the transfer function of one of the warm quadrupole magnet in the vicinity of the test setup



- Still, small compared to required dynamic beta-beat of $\Delta\beta/\beta|_{\max} < 20\%$

- Squeezing from $\beta^* = 10 \text{ m} \rightarrow \beta^* = 2 \text{ m}$ in all four IPs



- Nodes at optics matching points & leakage of squeeze of about 5% in IR7
- For the time being considered as small and compatible with present collimation requirements for low-intensity beams in the LHC.
- N.B. Meas. much noisier due the reduced signal-to-noise ratio during the β^* -squeeze of only 16 dB (reduced excitation strength at top energy + small bunch intensity)

- The aim of the continuous beta-beat measurement studies at the LHC was to
 - provide a proof-of-feasibility for the measurement technique, and
 - to assess magnitude and time-scale of the LHC lattice changes.
- Continuous beta-beat measurement system could achieve a 1% resolution
 - only limited by the maximum off-resonance excitation power, and
 - for excitations being kept below a micro-meter
→ transparent for nominal LHC operation.
- 2010 measurements seem to confirm that fill-to-fill beta-beating is reproducible within 1% – provided machine underwent a nominal pre-cycle
- Present SPS/LHC installation using 3dB-Splitters works fine for a few pick-up locations but does not scale well (costs) for massive deployment (dominated by HF cabling, connector, mechanics, etc...)
- If there is some interest/requirement: should and needs be specified as part of a future BPM system at an early stage, e.g. SPS MOPOS renovation & future LHC BPM upgrade



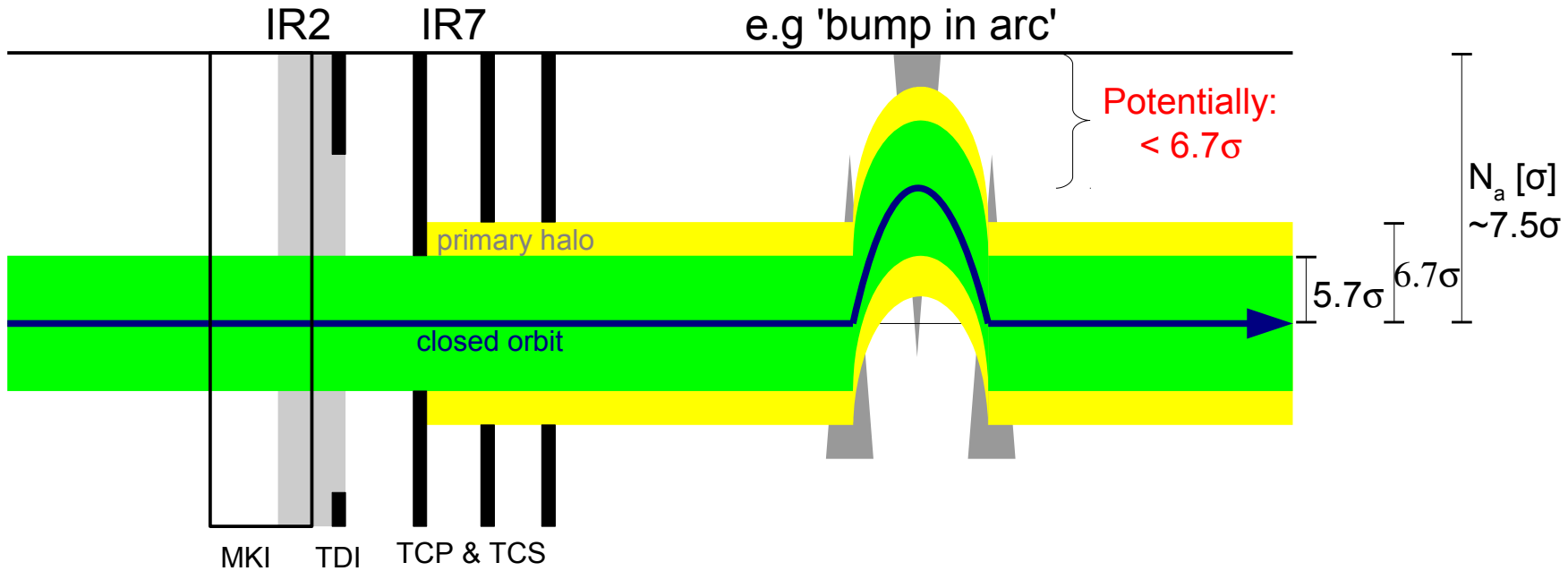
additional supporting slides

- Beta-Beat Sources
 - Quadrupole gradient and Momentum errors
 - Feed-down due to off-centre horizontal orbit in lattice sextupoles
 -

- Requirements: Brüning, Fartoukh, *LHC Project Report 501*

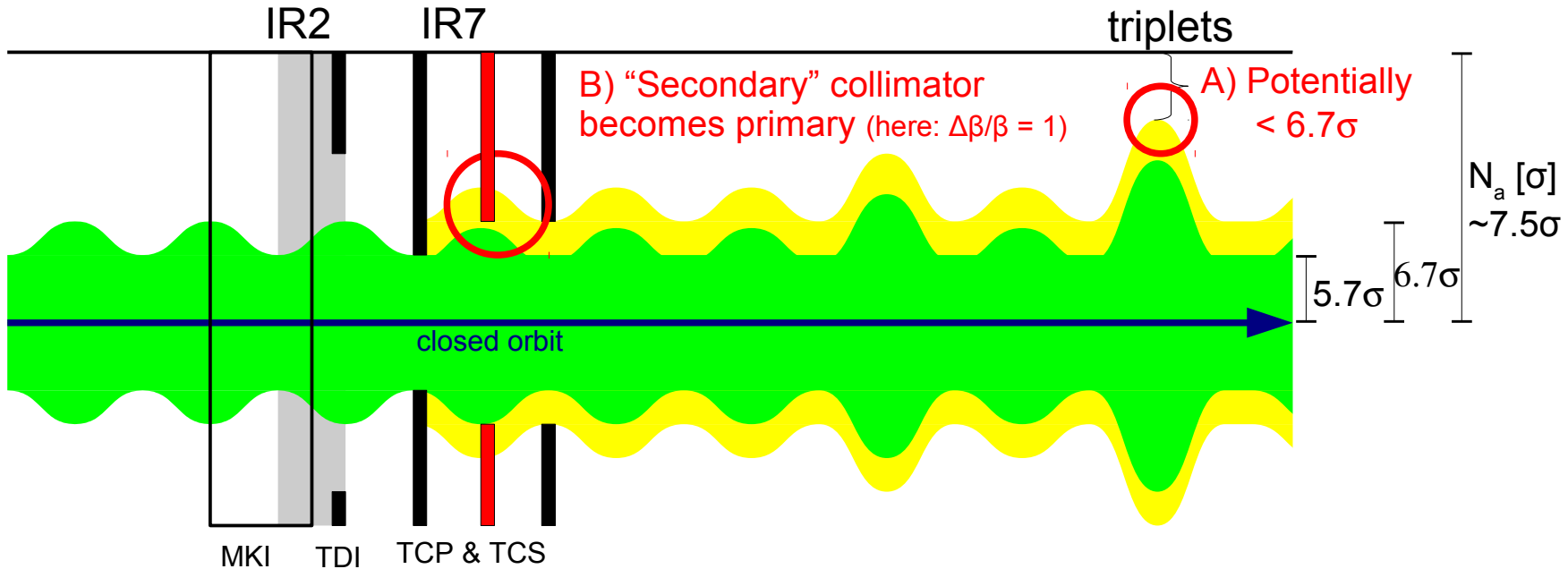
Peak hor. β -beating [%]	Mechanical aperture	14 / 15 (inj. / col.)
Peak vert. β -beating [%]	Mechanical aperture	16 / 19 (inj. / col.)
R.M.S. hor. β -beating [%]	Mechanical aperture	4.8 / 5.2 (inj. / col.)
R.M.S. vert.. β -beating [%]	Mechanical aperture	5.5 / 6.6 (inj. / col.)

- Combined failure: Local orbit bump and collimation efficiency (/kicker failure):



- To guarantee two stage cleaning efficiency/machine protection:
 - Local: TCP must be $>0.7\sigma$ closer than TCS w.r.t. the beam \rightarrow Orbit FB
 - Global: no other object (except TCP) closer to beam than TCS
- \rightarrow Orbit bumps may compromise function of machine protection/collimation
- \rightarrow tackled by LHC Orbit Feedback

- Combined failure: beta-beat and collimation efficiency



- “Collimator gap must be 10 times smaller than available triplet aperture!”¹

$$a_{coll} \leq a_{triplet} \cdot \sqrt{\frac{\beta_{coll}}{\beta_{triplet}}} \cdot \left(\frac{A_{primary}^{max}}{A_{secondary}^{max}} \right)$$

~ 0.15 ~ 0.6

A) β -Beat reduces required protection: $\Delta\beta/\beta \approx 20\% \rightarrow 20\%$ tighter collimator settings

B) β -Beat reduces cleaning performance

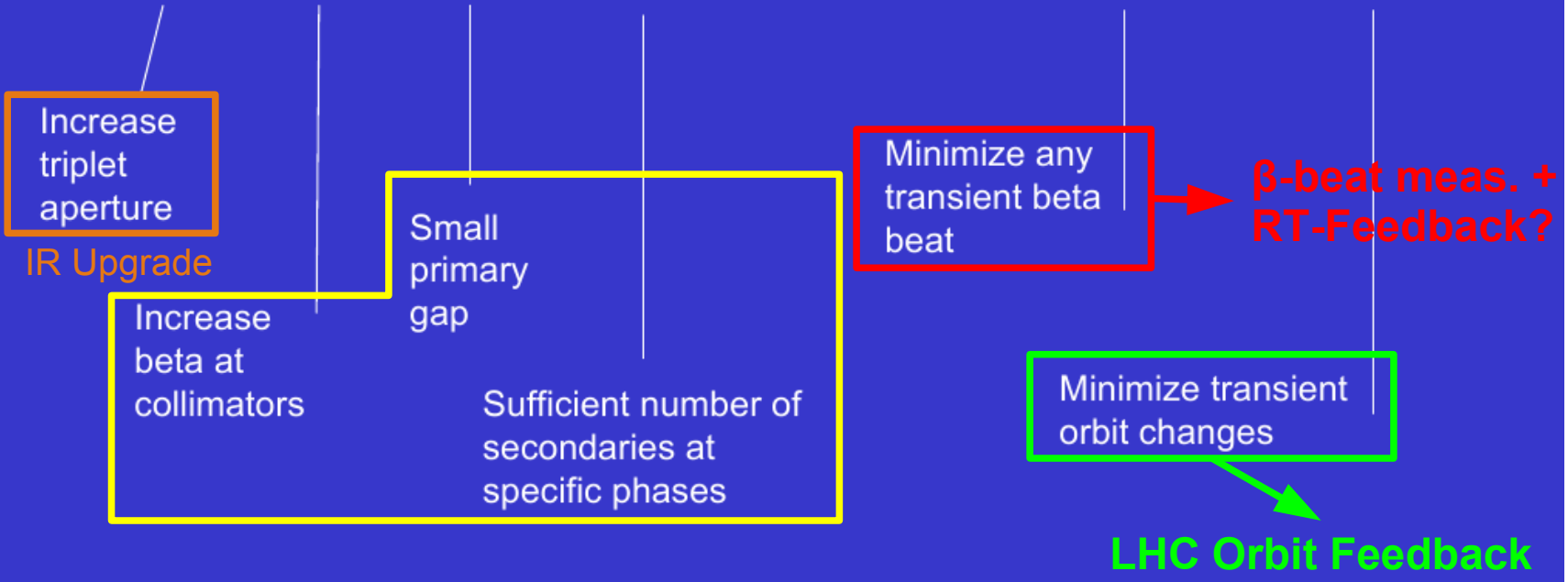
¹ R. Assmann, “Collimation and Cleaning: Could this limit the LHC Performance?”, Chamonix XII, 2003

Performance Limitations & Constraints on β^*

If retraction is adjusted such to allow some maximum transient beta beat and orbit error, then **constraint of β^*** :

N.B. $C = \beta_{trip} \cdot \beta^*$

$$\beta^* \geq \frac{C^2}{a_{triplet}^2 \cdot \beta_{coll}} \cdot \left(n_{prim} + \Delta A_{max} + 1.7 \cdot \left[n_{prim} \cdot \sqrt{\frac{\Delta\beta_{max}}{\beta_0}} + \frac{\Delta x_{orbit}^{max}}{\sigma_x} \right] \right)^2$$



Larger β^* - A way to relax operational collimator tolerances!

(However, loose passive protection)