

# Longitudinal Painting for a PSB H- Injection



C. Carli

- H<sup>-</sup> injection at other places around the world
- Basic facts and considerations for Linac 4 and PSB
  - Bunching factor and  $d(B\rho)/dt$
  - Painting and finite dispersion at PSB injection
  - Effect of  $d(B\rho)/dt$  energy of "synchronous particle"
- Schemes investigated:
  - Three energy slices
  - Painting with fast sinusoidal energy modulation
  - Painting with slow sinusoidal energy modulation
  - Triangular energy modulation
- Energy modulation
- Summary and Outlook

Acknowledgements:

Based on many discussions with R. Garoby, Frank, Giulia, Alessandra, Michel ...

# H<sup>-</sup> injection at other places around the world



Collect information to avoid "re-inventing the wheel" !

- PDAC:
  - Injection lasts several (~9) synchrotron revolutions,
  - Synchrotron motion used for azimuthally smoothing,
  - Not applicable for PSB case (no way to inject over several synchrotron periods).
- SNS:
  - Rather awkward longitudinal distributions in some papers (on transverse painting), but relatively smooth bunch shape,
  - Only  $\frac{1}{4}$  of a synchrotron period for bunch shortening:
    - "Funny" bunch shape, but beam kept only very shortly (compared to pseudoadiabatic capture).
  - Thought about a "energy spreader" cavity !.
- J-PARC:
  - First glance similarities with H<sup>-</sup> injection into the PSB (Injection energy, ...),
  - Lasts several synchrotron oscillations (many turns, high RF voltage, harm.) !!

Conclusion:

- H<sup>-</sup> injection into PSB: somehow unique case for painting:
  - No way to profit from synchrotron motion for longitudinal painting.

# Basic Facts and Considerations

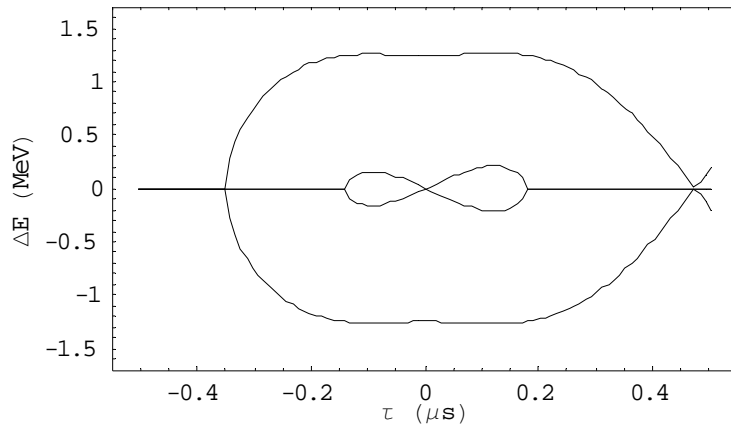


- Longitudinal acceptance, emittance ..... (cf F. Pedersen):
  - Aim: Favorable (large) bunching factor for "small" tune spread
  - Acceleration with full bucket and maximum RF voltage (i.e. large emittance):
    - For a given emittance: best bunching factor with acceptance just sufficient for emittance
    - Larger emittance (and RF voltage) results in smaller  $\varphi_s$ , larger bunching factor and smaller tune spread
  - Bdot a compromise between bunching factor and time spent at low energy:
    - Small Bdot -> smaller tune spread, but long time at low energy,
    - Large Bdot -> larger tune spread during a shorter time.
- $\partial B\rho/\partial t$  at injection:
  - Present situation (protons injected at 50 MeV):
    - Injection on ramp with  $\partial B\rho/\partial t = 4.0$  Tm/s,
    - Passage at 160 MeV with  $\partial B\rho/\partial t = 10$  Tm/s,
    - Maximum ramp  $\partial B\rho/\partial t > 16.0$  Tm/s (higher for 900 ms cycle ?)
  - Expectation for  $H^-$  for Linac 4:
    - $\partial B\rho/\partial t = 10$  Tm/s is upper limit,

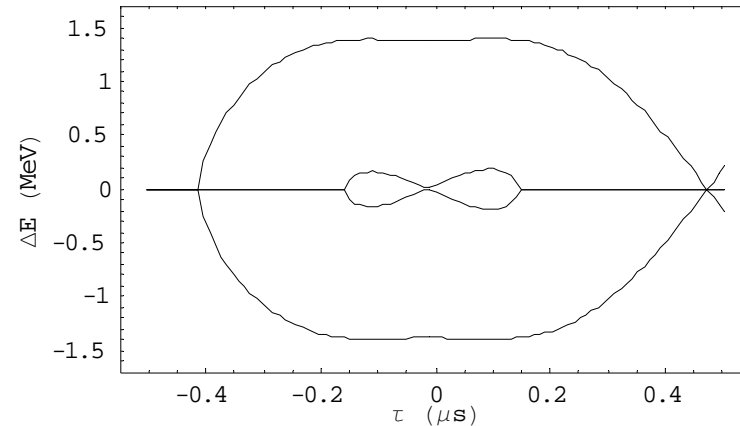
# Basic Facts and Considerations



- Bucket for maximum voltage ( $V_{h=1} = 8\text{kV}$ ,  $V_{h=2} = 5\text{kV}$ ) and expected  $\partial B\rho/\partial t$  :



$$\partial B\rho/\partial t = 10 \text{ Tm/s} \quad \Delta\phi = 203 \text{ deg}$$



$$\partial B\rho/\partial t = 5 \text{ Tm/s} \quad \Delta\phi = 191 \text{ deg}$$

- Little, but not negligible motion in longitudinal phase space:
  - No way to get painting for free from synchrotron motion,
  - "Active" (energy variation -amplitude  $\approx \pm 1.2\text{MeV}$ - and chopping) painting needed !
  - Necessary Amplitude of energy variation :  $\sim \pm 1.2 \text{ MeV}$
  - Attention: Acceptance of the transfer line !!
  - Synchrotron motion may lead to local density increases/increases,
  - Avoid slow painting in one direction (e.g. energy monotonously increasing) only

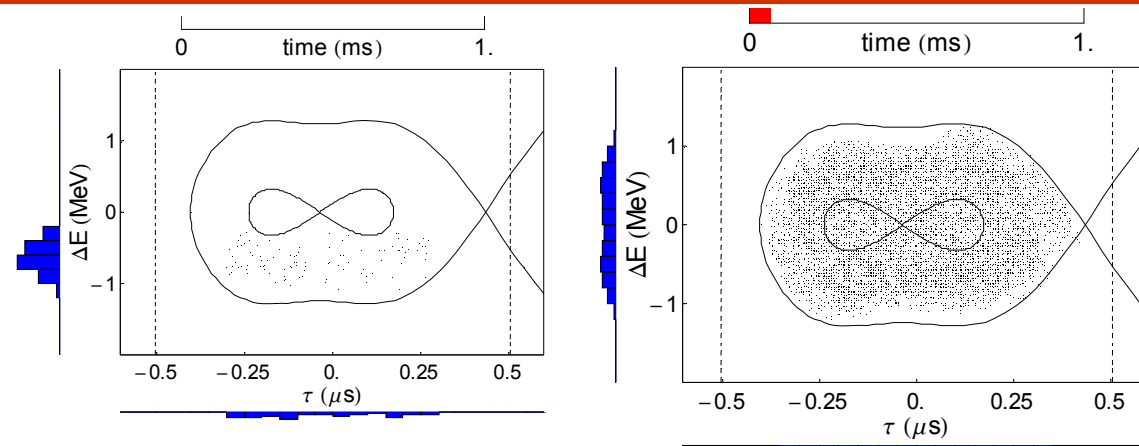
# Basic Facts and Considerations



- Energy of "synchronous particle increases during injection:
  - During 100 turns (high intensity) with  $\partial B\rho/\partial t = 10 \text{ Tm/s}$  :  $\approx 156 \text{ MeV}$
  - Adds to needs for energy modulation for injection into one ring,
  - Ring to ring variations compensated with "Bdl"s (orbit perturbations  $\sim 1\text{mm}$ ).
- Dispersion in injection straight section:
  - in case the injected beam arrives with  $D=0\text{m}$  (and  $D'=0$ ):
    - full bucket height:  $\sim 2 \text{ MeV}$ ,
    - rms momentum spread after injection:  $\frac{\sigma_p}{p} \approx \frac{1}{\beta_{rel}^2} \frac{2 \text{ MeV} / 5}{(938.27 + 160) \text{ MeV}} \approx 1.3 \cdot 10^{-3}$
    - horizontal emittance blow-up:  $\Delta \varepsilon_{rms}^* \approx \beta_{rel} \gamma_{rel} \frac{1}{2} \frac{(D(\sigma_p/p))^2}{\beta_{Twiss}} \approx 0.2 \mu\text{m}$
    - May be acceptable (thus injected beam arriving with  $D=0\text{m}$  may be o.k.)
    - Better be careful (previous computation led to opposite result) !!
    - matched D at injection -> larger beam, more foil hits ... !?
- Number of injected turns:
  - Painting in three phase spaces with only 9 injected turns (actual figure for LHC) ?
  - Are in-homogeneities (unavoidable painting with few turns) a problem ?
  - Lengthen injection (at least for low intensities) ?
  - Painting in all three phase spaces for  $H^-$  in PSB a non-trivial problem:
    - Keep conventional pseudo-adiabatic capture as plan B.

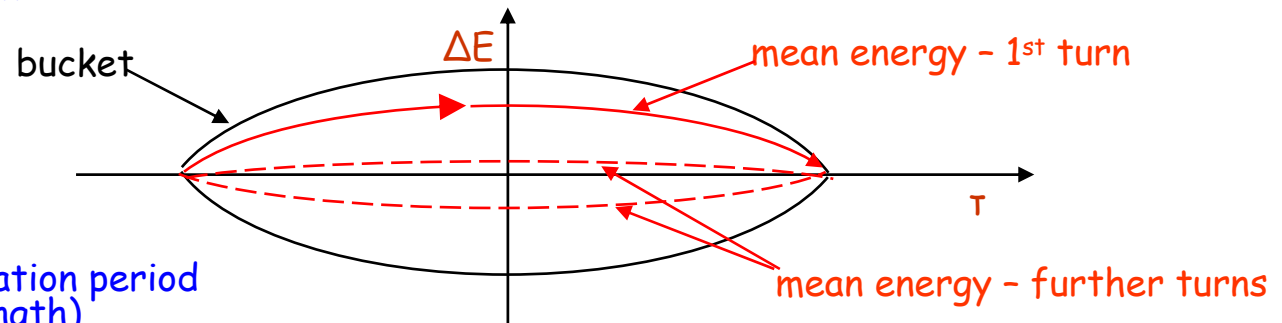
# Schemes investigated

- Three energy slices:



- Simple (robust) scheme:
- Just three different energies to be delivered,
- Reasonably smooth (better than pseudo-adiabatic bunching) filling of the bucket.
- Abandoned: energy modulation out of reach for Linac 4
- Fast sinusoidal energy modulation:

- Aimed at painting the bucket border,



- Abandoned:
  - Restrictive (modulation period matches bucket length),
  - Creation of the energy modulation

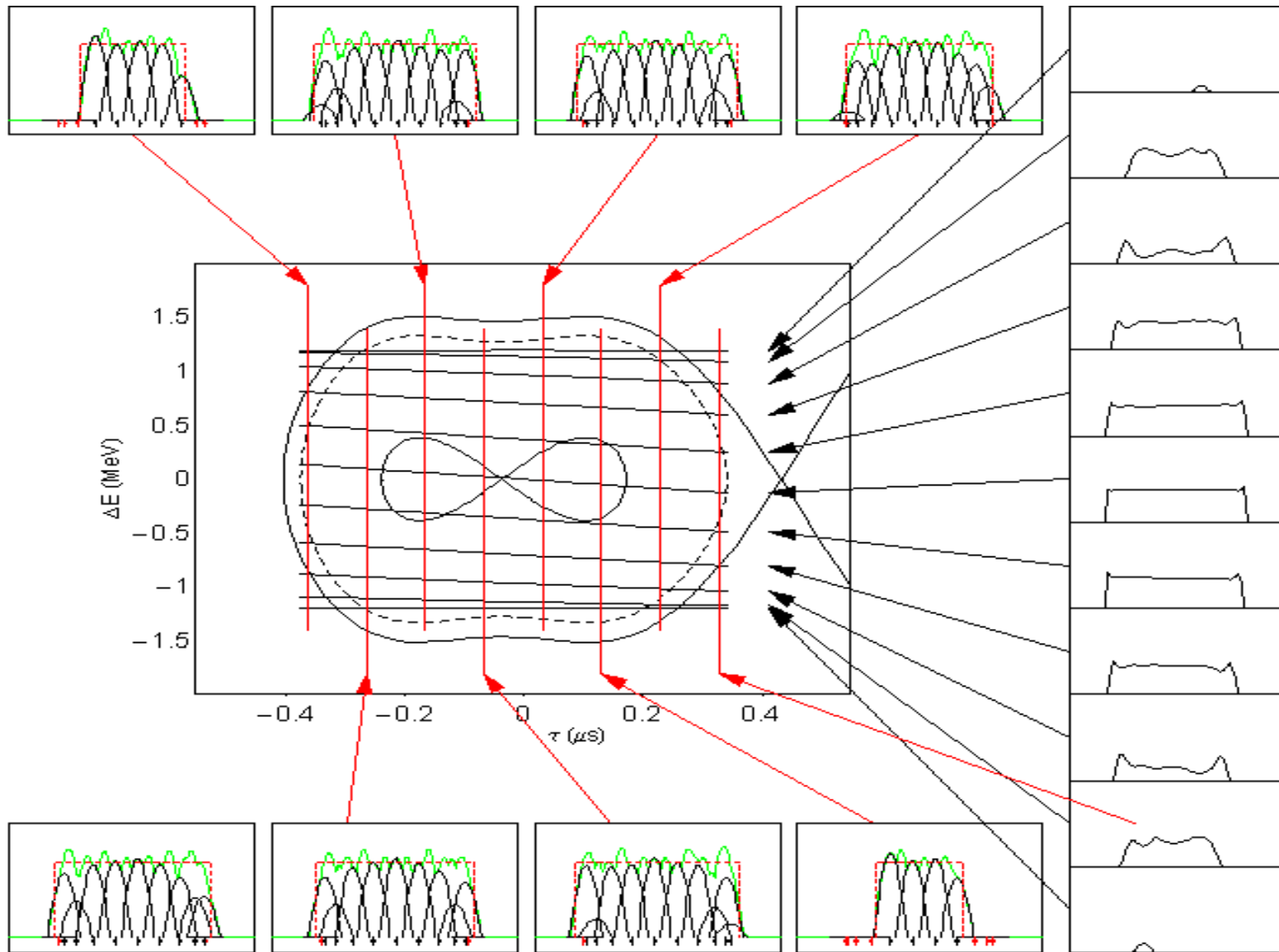
# Schemes investigated

## (Slow Sinusoidal energy modulation)



- Initial idea:
  - Slow sinusoidal energy modulation:
    - Say one modulation period takes 20 PSB revolutions (e.g. instead of 9 turns for LHC beams),
  - Algorithm to compute which bunches are taken and which are kicked out by chopper.
- Approach:
  - For fixed longitudinal position,
    - Energy offset at different turns given,
    - Aim at painting a given fraction (say 80%) of the acceptance homogeneously
  - First step: current versus time curves (to be translated into bunch structure -giving right mean current vs time- later)
- Result (plots on following pages):
  - Looks reasonable at a first glance:
    - critical at bucket borders and for large  $\sigma_E$
- Abandoned
  - How to generate energy modulation?

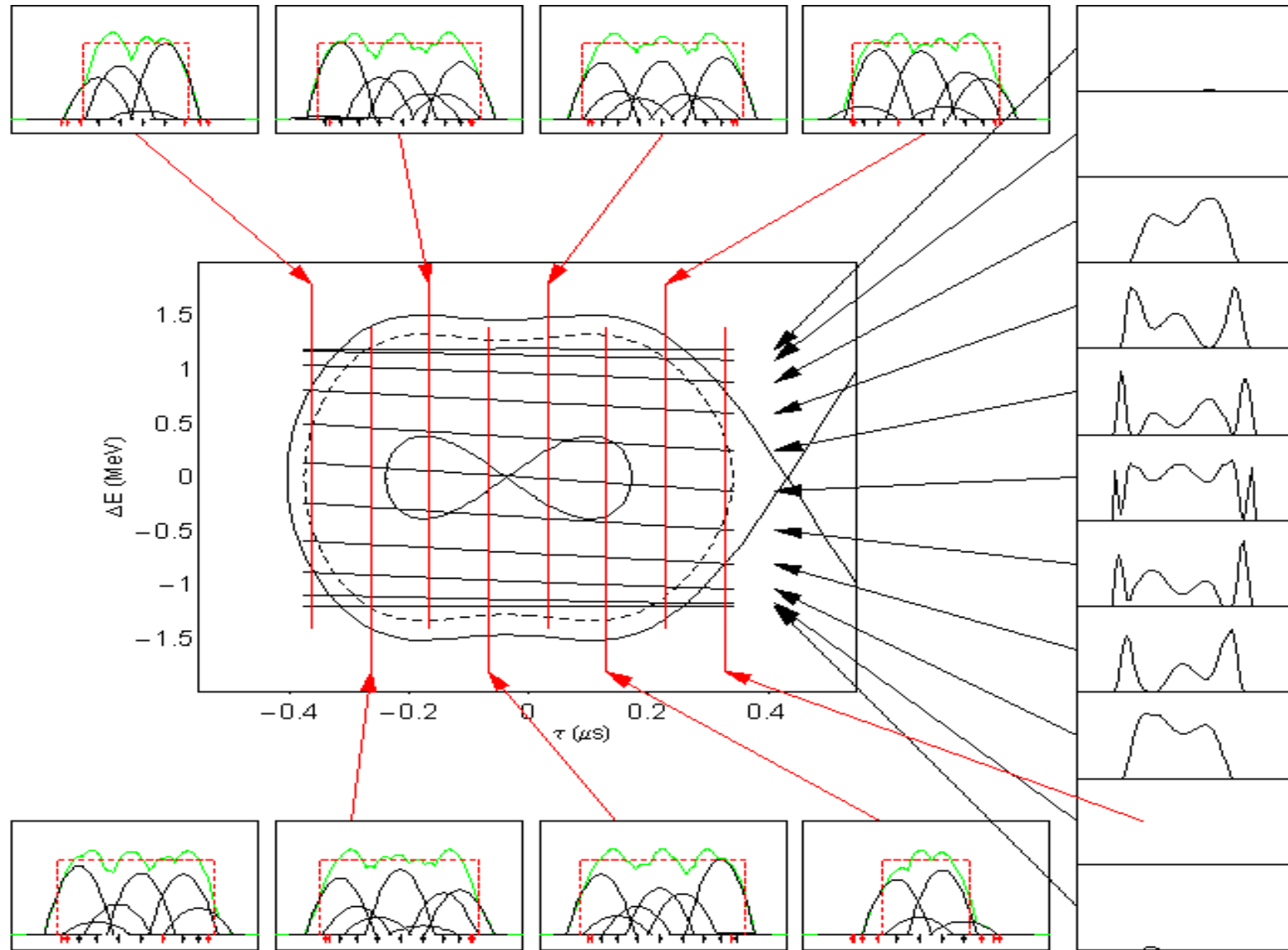
# Schemes investigated (Slow Sinusoidal energy modulation)



Amplitude = 1.200 MeV,  $\sigma_E = .120$  MeV



# Schemes investigated (Slow Sinusoidal energy modulation)



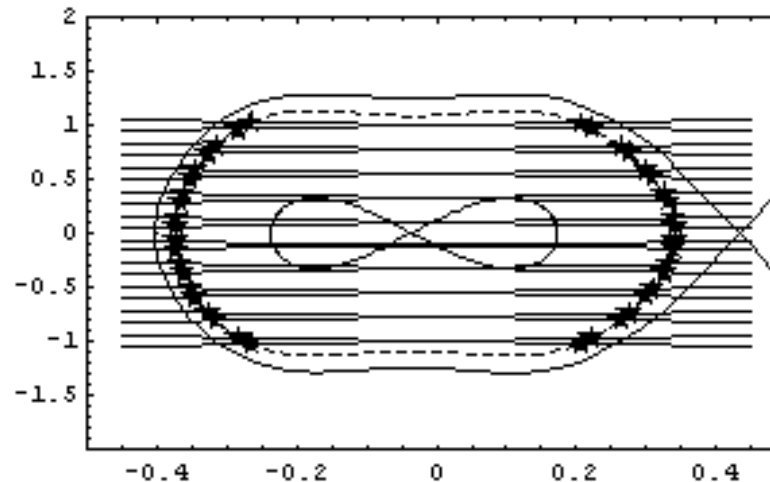
Amplitude = 1.200 MeV,  $\sigma_E = .250$  MeV

# Schemes investigated (Triangular)



- Motivation:

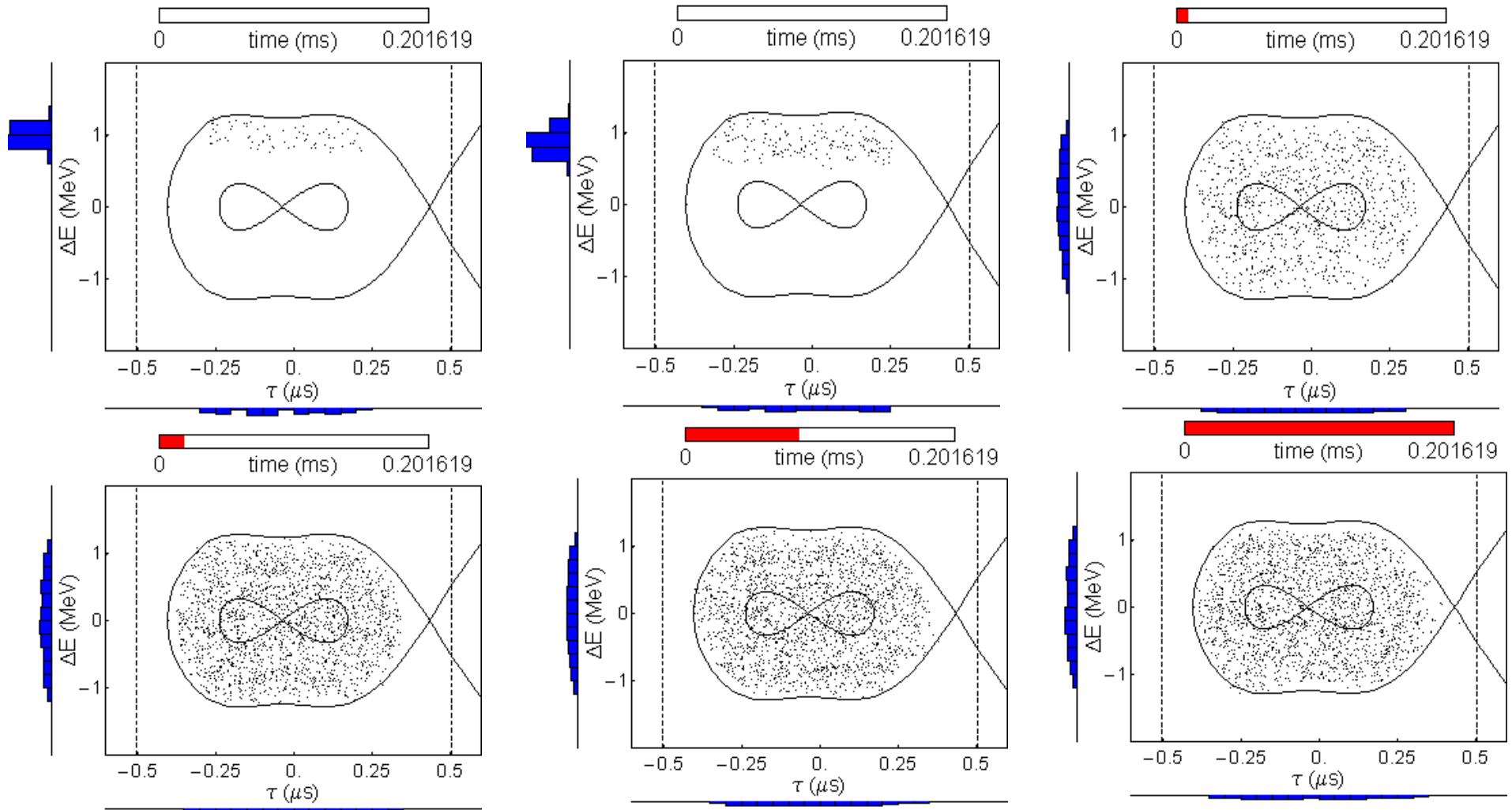
- initial ideas (see below) on energy ramping ruled out,
- linear ramp (energy vs time):
  - "simple" for generation of E modulation,
  - turn-by-turn equidistance.
- Switching the beam on/off inside/outside a contour (for present simulations 80% of acceptance) in longitudinal phase space



- Result:

- Only promising scheme (in simulations without direct space charge),
- Further simulations (see last slide).

# Schemes investigated (Triangular Energy Modulation)



Longitudinal phase after 1, 2, 10, 20 (end of injection), ~100 and 200 revolutions

# Energy Modulation



- Slow sinusoidal modulation based on:
  - Ramping just after Linac 4: Sinusoidal phase modulation at debuncher,
  - Ramping after debuncher: ramping disturbs debunching
  - No way - find another scheme !
  - Rule out envisaged painting schemes !
- Phase modulation (like Linac 3 ramping for LEIR):
  - Needs:  $\sim 1.2$  MV in  $10 \mu\text{s}$  (LEIR  $\sim 0.1$  MV in  $200 \mu\text{s}$ ),
  - Energy modulation cavity:
    - Say cavity right after Linac with amplitude  $A_U = 2.4$  MV,
    - $\pm 1.2$  MV corresponds to  $\pm 30$  deg (60 deg phase shift in  $10 \mu\text{s}$ ),
    - Ramp up down corresponds to frequency offsets of  $\Delta f \approx \pm 17$  kHz.
  - Debuncher (distance  $l$  downstream):
    - $\Delta E = \pm 1.2$  MV  $\rightarrow \Delta t = (1.89 \cdot 10^{-11} \text{ s/m}) l \rightarrow \Delta \phi = 2.39 \text{ deg/m}$
    - Very likely to be a limitation (showstopper ?): compromise between distance and maximum phase excursion !!
    - Phase excursion  $< \pm 60$  deg ( $\Delta f < 35$  kHz)  $\rightarrow l < 20$  m
  - Giulia and Alessandra are looking into this !



# Summary and Outlook

- Summary:
  - H- injection into PSB somewhat unique for long. painting,
  - Injection with dispersion and (very likely)  $B\dot{\theta}$ ,
  - Several schemes investigated,
  - Slow triangular energy modulation most promising.
- Next:
  - How to generate energy modulation (is linear ramp feasible ?),
  - Include space charge (how ?, ESME suitable ? ...),
  - Energy jitter:
    - Pulse to pulse or bunch to bunch (quantify with Energy modulation) ?
    - Can PSB phase loop compensate a pulse to pulse jitter ?
  - Add transverse phase space:
    - effect of dispersion (resulting emittance blow-up, correlation between horizontal and vertical phase space),
    - number of injected turns and painting in 6D phase space,
    - consequences for stripping foil ... ,
  - Injection line with energy modulation:
    - acceptance,
    - dispersion (horizontal AND vertical), chromatic effects ...